<span id="page-0-0"></span>

# *The Open Source CFD Toolbox*

# Tutorial Guide

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# <span id="page-8-0"></span>**Contents**







# <span id="page-12-0"></span>Chapter 1

# Introduction

This guide details the process of setup, simulation and post-processing for some Open-FOAM test cases, with the principal aim of introducing a user to the basic procedures of running OpenFOAM. The **\$FOAM\_TUTORIALS** directory contains many more cases that demonstrate the use of all the solvers and many utilities supplied with OpenFOAM. Before attempting to run the tutorials, the user must first make sure that they have installed OpenFOAM correctly.

The tutorial cases describe the use of the blockMesh pre-processing tool, case setup and running OpenFOAM solvers and post-processing using paraFoam. Those users with access to third-party post-processing tools supported in OpenFOAM have an option: either they can follow the tutorials using paraFoam; or refer to the User Guide for details on post-processing with external applications.

Copies of all tutorials are available from the tutorials directory of the OpenFOAM installation. The tutorials are organised into a set of directories according to the type of flow and then subdirectories according to solver. For example, all the icoFoam cases are stored within a subdirectory *incompressible/icoFoam*, where *incompressible* indicates the type of flow. If the user wishes to run a range of example cases, it is recommended that the user copy the *tutorials* directory into their local *run* directory. They can be easily copied by typing:

mkdir -p \$FOAM RUN cp -r \$FOAM\_TUTORIALS \$FOAM\_RUN

## <span id="page-12-1"></span>1.1 Getting started

An OpenFOAM case requires definitions for the mesh, initial fields, physical models, control parameters, etc. As described in the User Guide section [2.1,](#page-15-0) OpenFOAM data is stored in a set of files within a case directory rather than in a single case file. The case directory is given a suitably descriptive name, e.g. the first example case for this tutorial guide is simply named cavity, under which the required information is located in the three directories:

- constant
- system, and
- $\bullet$  initial time directory, e.g.O.

Editing files is possible in OpenFOAM because the I/O uses a plain text dictionary format with keywords that convey sufficient meaning to be understood by even the least experienced users. Many editors are available for both Linux and Windows environments, e.g. on Ubuntu the default GUI-based editor is gedit, and default terminal editor is nano. Other popular text editors include vim, emacs, kate, and atom.

## <span id="page-13-0"></span>1.1.1 Note for Windows Users

When using a shared directory, e.g. between Windows and Docker, users may prefer to use a Windows-based text editor. However, care should be taken not to change the encoding of the text files to ensure that they remain readable by OpenFOAM. Good choices may be atom and PSPad — both are free and automatically keep the correct encoding.

# <span id="page-14-0"></span>Chapter 2

# Incompressible flow

## <span id="page-15-0"></span>2.1 Lid-driven cavity flow

Tutorial path:

## • \$FOAM\_[TUTORIALS/incompressible/icoFoam/cavity/cavity](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/incompressible/icoFoam/cavity/cavity)

This tutorial will describe how to pre-process, run and post-process a case involving isothermal, incompressible flow in a two-dimensional square domain. The geometry is shown in Figure [2.1](#page-15-3) in which all the boundaries of the square are walls. The top wall moves in the x-direction at a speed of  $1 \text{ m/s}$  while the other 3 are stationary. Initially, the flow will be assumed laminar and will be solved on a uniform mesh using the icoFoam solver for laminar, isothermal, incompressible flow. During the course of the tutorial, the effect of increased mesh resolution and mesh grading towards the walls will be investigated. Finally, the flow Reynolds number will be increased and the pisoFoam solver will be used for turbulent, isothermal, incompressible flow.



<span id="page-15-3"></span>Figure 2.1: Geometry of the lid driven cavity.

## <span id="page-15-1"></span>2.1.1 Pre-processing

In preparation of editing case files and running the first cavity case, the user should change to the case directory

cd \$FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavity

## <span id="page-15-2"></span>2.1.1.1 Mesh generation

OpenFOAM always operates in a 3 dimensional Cartesian coordinate system and all geometries are generated in 3 dimensions. OpenFOAM solves the case in 3 dimensions by default but can be instructed to solve in 2 dimensions by specifying a 'special' empty boundary condition on boundaries normal to the (3rd) dimension for which no solution is required. Here, the mesh must be 1 cell layer thick, and the empty patches planar.

The cavity domain consists of a square of side length  $d = 0.1$  m in the x-y plane. A uniform mesh of 20 by 20 cells will be used initially. The block structure is shown in Figure [2.2.](#page-16-0) The blockMesh mesh generator supplied with OpenFOAM generates meshes from a description specified in an input dictionary, **blockMeshDict** located in the **system** directory for a given case. The **blockMeshDict** entries for this case are as follows:



<span id="page-16-0"></span>Figure 2.2: Block structure of the mesh for the cavity.

```
1 /*--------------------------------*- C++ -*----------------------------------*\
 2 | ========= | |
 3 | \\ / F ield | OpenFOAM: The Open Source CFD Toolbox |
4 | \setminus / 0 peration | Version: v2006<br>5 | \setminus / A nd | Website: www.org
5 | \sqrt{7} A nd | Website: www.openfoam.com
6 | \setminus\setminus M anipulation |
 7 \*---------------------------------------------------------------------------*/
\begin{array}{cc}\n7 & \times \rightarrow \rightarrow \rightarrow \rightarrow \rightarrow \\
8 & \text{FoamFile} \\
9 & 4\n\end{array}\begin{array}{cc} 9 & \textbf{\textsterling} \\ 10 & \end{array}10 version 2.0;<br>
11 format ascii;
\begin{array}{ccc} 11 & \text{format} \\ 12 & \text{class} \end{array}12 class dictionary;
13 object blockMeshDict;
\begin{array}{cc} 14 & & \\ 15 & // \end{array}15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 0.1;
18
\frac{19}{20} vertices
\frac{20}{21}21 (0 0 0)
22 (1 0 0)
23 (1 1 0)
24 (0 \ 1 \ 0)25 (0 0 0.1)
26 (1 0 0.1)
27 (1 1 0.1)
28 (0 1 0.1)
\begin{array}{c} 28 \\ 29 \end{array} ) ;
30
31 blocks
\frac{32}{33} (
           hex (0 1 2 3 4 5 6 7) (20 20 1) simpleGrading (1 1 1)
34 );
35
36 edges
37 (
\begin{array}{cc} 37 & ( \\ 38 & ) \end{array}39
40 boundary
\begin{array}{cc} 41 & \textcircled{\scriptsize 42} \\ 42 & \textcircled{\scriptsize 12} \end{array}movingWall
\begin{matrix} 43 \\ 44 \end{matrix} \qquad \qquad \begin{matrix} \hspace{-.5cm} \{ \end{matrix}44 type wall;<br>45 faces
                 \det faces
\frac{46}{47}\frac{47}{48} (3 7 6 2)
\frac{4i}{48} );
\begin{array}{ccc} 49 & & & \end{array}<br>50 f
50 fixedWalls
51 {
52 type wall;
53 faces
54 (
55 (0 4 7 3)
(2 \t6 \t5 \t1)57 (1\ 5\ 4\ 0)
```


The file first contains header information in the form of a banner (lines 1-7), then file information contained in a FoamFile sub-dictionary, delimited by curly braces  $({\{\ldots\}})$ .

For the remainder of the manual:

For the sake of clarity and to save space, file headers, including the banner and FoamFile sub-dictionary, will be removed from verbatim quoting of case files

The file first specifies the list of coordinates representing the block vertices; These are in arbitrary units, and can be scaled to the real problem dimensions using the scale entry, e.g.

scale 0.1;

The next section defines the **blocks** (here, only 1) using the vertex indices, *i.e.* index 0 for vertex 0, index 1 for vertex 1, and so on, and the number of cells within it in each of the 3 co-ordinate directions, and the cell spacing. The final section defines the boundary patches. Please refer to the User Guide section 4.3 to understand the meaning of the entries in the blockMeshDict file.

The mesh is generated by running blockMesh on this *blockMeshDict* file. From within the case directory, this is done, simply by typing in the terminal:

#### blockMesh

The running status of blockMesh is reported in the terminal window. Any mistakes in the blockMeshDict file are picked up by blockMesh and the resulting error message directs the user to the line in the file where the problem occurred. There should be no error messages at this stage.

#### <span id="page-17-0"></span>2.1.1.2 Boundary and initial conditions

Once the mesh generation is complete, the user can look at this initial fields set up for this case. The case is set up to start at time  $t = 0$  s, so the initial field data is stored in a 0 sub-directory of the cavity directory. The 0 sub-directory contains 2 files,  $p$  and U, one for each of the pressure  $(p)$  and velocity  $(U)$  fields whose initial values and boundary conditions must be set. Let us examine file  $p$ :

```
17 dimensions [0 2 - 2 0 0 0 0];
18
19 internalField uniform 0;
20
21 boundaryField
22 {
23 movingWall
```

```
24 {
25 type zeroGradient;
26 }
27
28 fixedWalls
29 {
30 type zeroGradient;
31 }
32
33 frontAndBack
34 {
35 type empty;
36 }
37 }
38
39 // ************************************************************************* //
```
There are 3 principal entries in field data files:

- dimensions specifies the dimensions of the field, here *kinematic* pressure, *i.e.*  $m^2 s^{-2}$  (see User Guide section 2.2.6 for more information);
- internalField the internal field data which can be uniform, described by a single value; or nonuniform, where all the values of the field must be specified (see User Guide section 2.2.8 for more information);
- boundaryField the boundary field data that includes boundary conditions and data for all the boundary patches (see User Guide section 2.2.8 for more information).

For this case cavity, the boundary consists of walls only, split into 2 patches named: (1) fixedWalls for the fixed sides and base of the cavity;  $(2)$  movingWall for the moving top of the cavity. As walls, both are given a zeroGradient boundary condition for p, meaning "the normal gradient of pressure is zero". The frontAndBack patch represents the front and back planes of the 2D case and therefore must be set as empty.

In this case, as in most we encounter, the initial fields are set to be uniform. Here the pressure is kinematic, and as an incompressible case, its absolute value is not relevant, so is set to uniform 0 for convenience.

The user can similarly examine the velocity field in the  $0/U$  file. The dimensions are those expected for velocity, the internal field is initialised as uniform zero, which in the case of velocity must be expressed by 3 vector components, *i.e.*uniform (0 0 0) (see User Guide section [2.2.5](#page-48-1) for more information).

The boundary field for velocity requires the same boundary condition for the front-AndBack patch. The other patches are walls: a no-slip condition is assumed on the fixedWalls, hence a fixedValue condition with a value of uniform (0 0 0). The top surface moves at a speed of 1 m/s in the x-direction so requires a fixed Value condition also but with uniform (1 0 0).

#### <span id="page-18-0"></span>2.1.1.3 Physical properties

The physical properties for the case are stored in dictionaries whose names are given the suffix ... Properties, located in the Dictionaries directory tree. For an icoFoam case, the only property that must be specified is the kinematic viscosity which is stored from the transportProperties dictionary. The user can check that the kinematic viscosity is set correctly by opening the transportProperties dictionary to view/edit its entries. The keyword for kinematic viscosity is nu, the phonetic label for the Greek symbol  $\nu$  by which it is represented in equations. Initially this case will be run with a Reynolds number of 10, where the Reynolds number is defined as:

$$
Re = \frac{d|\mathbf{U}|}{\nu} \tag{2.1}
$$

where d and |U| are the characteristic length and velocity respectively and  $\nu$  is the kinematic viscosity. Here  $d = 0.1$  m,  $|\mathbf{U}| = 1$  ms<sup>-1</sup>, so that for  $Re = 10$ ,  $\nu = 0.01$  m<sup>2</sup>s<sup>-1</sup>. The correct file entry for kinematic viscosity is thus specified below:

```
17
18 nu 0.01;
19
20
21 // ************************************************************************* //
```
### <span id="page-19-0"></span>2.1.1.4 Control

Input data relating to the control of time and reading and writing of the solution data are read in from the *controlDict* dictionary. The user should view this file; as a case control file, it is located in the system directory.

The start/stop times and the time step for the run must be set. OpenFOAM offers great flexibility with time control which is described in full in the User Guide section 6.1. In this tutorial we wish to start the run at time  $t = 0$  which means that OpenFOAM needs to read field data from a directory named  $0$  — see User Guide section [2.1](#page-15-0) for more information of the case file structure. Therefore we set the startFrom keyword to startTime and then specify the startTime keyword to be 0.

For the end time, we wish to reach the steady state solution where the flow is circulating around the cavity. As a general rule, the fluid should pass through the domain 10 times to reach steady state in laminar flow. In this case the flow does not pass through this domain as there is no inlet or outlet, so instead the end time can be set to the time taken for the lid to travel ten times across the cavity, i.e. 1 s; in fact, with hindsight, we discover that 0.5 s is sufficient so we shall adopt this value. To specify this end time, we must specify the stopAt keyword as endTime and then set the endTime keyword to 0.5.

Now we need to set the time step, represented by the keyword deltaT. To achieve temporal accuracy and numerical stability when running icoFoam, a Courant number of less than 1 is required. The Courant number is defined for one cell as:

<span id="page-19-1"></span>
$$
Co = \frac{\delta t |\mathbf{U}|}{\delta x} \tag{2.2}
$$

where  $\delta t$  is the time step, |U| is the magnitude of the velocity through that cell and  $\delta x$ is the cell size in the direction of the velocity. The flow velocity varies across the domain and we must ensure  $Co < 1$  everywhere. We therefore choose  $\delta t$  based on the worst case: the maximum Co corresponding to the combined effect of a large flow velocity and small cell size. Here, the cell size is fixed across the domain so the maximum Co will occur next to the lid where the velocity approaches 1 m s<sup>−</sup><sup>1</sup> . The cell size is:

$$
\delta x = \frac{d}{n} = \frac{0.1}{20} = 0.005 \text{ m} \tag{2.3}
$$

Therefore to achieve a Courant number less than or equal to 1 throughout the domain the time step deltaT must be set to less than or equal to:

$$
\delta t = \frac{Co \ \delta x}{|\mathbf{U}|} = \frac{1 \times 0.005}{1} = 0.005 \ \mathrm{s}
$$
\n
$$
(2.4)
$$

As the simulation progresses we wish to write results at certain intervals of time that we can later view with a post-processing package. The writeControl keyword presents several options for setting the time at which the results are written; here we select the timeStep option which specifies that results are written every nth time step where the value  $n$  is specified under the writeInterval keyword. Let us decide that we wish to

write our results at times  $0.1, 0.2,..., 0.5$  s. With a time step of  $0.005$  s, we therefore need to output results at every 20th time time step and so we set writeInterval to 20.

OpenFOAM creates a new directory named after the current time, e.g. 0.1 s, on each occasion that it writes a set of data, as discussed in full in User Guide section [2.1.](#page-15-0) In the icoFoam solver, it writes out the results for each field, U and p, into the time directories. For this case, the entries in the controlDict are shown below:



## <span id="page-20-0"></span>2.1.1.5 Discretisation and linear-solver settings

The user specifies the choice of finite volume discretisation schemes in the  $f\nu$ Schemes dictionary in the **system** directory. The specification of the linear equation solvers and tolerances and other algorithm controls is made in the *fvSolution* dictionary, similarly in the system directory. The user is free to view these dictionaries but we do not need to discuss all their entries at this stage except for pRefCell and pRefValue in the PISO sub-dictionary of the *fvSolution* dictionary. In a closed incompressible system such as the cavity, pressure is relative: it is the pressure range that matters not the absolute values. In cases such as this, the solver sets a reference level by pRefValue in cell pRefCell. In this example both are set to 0. Changing either of these values will change the absolute pressure field, but not, of course, the relative pressures or velocity field.

## <span id="page-20-1"></span>2.1.2 Viewing the mesh

Before the case is run it is a good idea to view the mesh to check for any errors. The mesh is viewed in paraFoam, the post-processing tool supplied with OpenFOAM. The paraFoam post-processing is started by typing in the terminal from within the case directory

#### paraFoam

Alternatively, it can be launched from another directory location with an optional -case argument giving the case directory, e.g.

#### paraFoam -case \$FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavity

This launches the ParaView window as shown in Figure ??. In the Pipeline Browser, the user can see that ParaView has opened cavity.OpenFOAM, the module for the cavity case. Before clicking the Apply button, the user needs to select some geometry from the Mesh Parts panel. Because the case is small, it is easiest to select all the data by checking the box adjacent to the Mesh Parts panel title, which automatically checks all individual components within the respective panel. The user should then click the Apply button to load the geometry into ParaView. Some general settings are applied as described in User Guide section 7.1.7.1. Please consult this section about these settings.

The user should then open the Properties panel that controls the visual representation of the selected module. Within the Display panel the user should do the following as shown in Figure [2.3:](#page-21-0) (1) set Color By Solid Color; (2) click Edit and select an appropriate colour e.g. black (for a white background); (3) select Wireframe from the Representation menu. The background colour can be set by selecting Settings... from Edit in the top menu panel.



<span id="page-21-0"></span>Figure 2.3: Viewing the mesh in paraFoam.

Especially the first time the user starts ParaView, it is recommended that they manipulate the view as described in User Guide section 7.1.7. In particular, since this is a 2D case, it is recommended that Camera Parallel Projection is selected. To do so, click on the Toggle Advanced Properties to show the option towards the bottom on the panel.

The Orientation Axes can be toggled on and off in the Annotation window or moved by drag and drop with the mouse.

## <span id="page-22-0"></span>2.1.3 Running an application

Like any UNIX/Linux executable, OpenFOAM applications can be run in two ways: as a foreground process, i.e. one in which the shell waits until the command has finished before giving a command prompt; as a background process, one which does not have to be completed before the shell accepts additional commands.

On this occasion, we will run icoFoam in the foreground. The icoFoam solver is executed either by entering the case directory and typing

#### icoFoam

at the command prompt, or with the optional -case argument giving the case directory, e.g.

icoFoam -case \$FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavity

The progress of the job is written to the terminal window. It tells the user the current time, maximum Courant number, initial and final residuals for all fields.

## <span id="page-22-1"></span>2.1.4 Post-processing

As soon as results are written to time directories, they can be viewed using paraFoam. Return to the paraFoam window and select the Properties panel for the cavity.OpenFOAM case module. If the correct window panels for the case module do not seem to be present at any time, please ensure that: cavity.OpenFOAM is highlighted in blue; eye button alongside it is switched on to show the graphics are enabled;

To prepare paraFoam to display the data of interest, we must first load the data at the required run time of 0.5 s. If the case was run while ParaView was open, the output data in time directories will not be automatically loaded within ParaView. To load the data the user should click Refresh Times in the Properties window. The time data will be loaded into ParaView.

#### <span id="page-22-2"></span>2.1.4.1 Isosurface and contour plots

To view pressure, the user should open the Properties panel since it controls the visual representation of the selected module. To make a simple plot of pressure, the user should select the following, as described in detail in Figure [2.4:](#page-23-0) select Surface from the Representation menu; in the Coloring panel, select Color by  $\circ$  P and Rescale to Data Range. Now in order to view the solution at  $t = 0.5$  s, the user can use the VCR Controls or Current Time Controls to change the current time to 0.5. These are located in the toolbars below the menus at the top of the ParaView window, as shown in Figure ??. The pressure field solution has, as expected, a region of low pressure at the top left of the cavity and one of high pressure at the top right of the cavity as shown in Figure [2.5.](#page-23-1)

With the point icon  $( \cdot )$  the pressure field is interpolated across each cell to give a continuous appearance. Instead if the user selects the cell icon,  $\mathcal{P}_P$ , from the Coloring by menu, a single value for pressure will be attributed to each cell so that each cell will be denoted by a single colour with no grading.



<span id="page-23-0"></span>Figure 2.4: Displaying pressure contours for the cavity case.



<span id="page-23-1"></span>Figure 2.5: Pressures in the cavity case.

A colour bar can be included by either by clicking the Toggle Color Legend Visibility button in the Active Variable Controls toolbar, or by selecting Show Color Legend from the View menu. Clicking the Edit Color Map button, either in the Active Variable Controls toolbar or in the Color panel of the Display window, the user can set a range of attributes of the colour bar, such as text size, font selection and numbering format for the scale. The colour bar can be located in the image window by drag and drop with the mouse.

New versions of ParaView default to using a colour scale of blue to white to red rather than the more common blue to green to red (rainbow). Therefore the first time that the user executes ParaView, they may wish to change the colour scale. This can be done by selecting Choose Preset in the Color Scale Editor and selecting Blue to Red Rainbow. After clicking the OK confirmation button, the user can click the Make Default button so that ParaView will always adopt this type of colour bar.

If the user rotates the image, they can see that they have now coloured the complete geometry surface by the pressure. In order to produce a genuine contour plot the user should first create a cutting plane, or 'slice', through the geometry using the Slice filter as described in User Guide section 7.1.8.1. The cutting plane should be centred at  $(0.05, 0.05, 0.005)$  and its normal should be set to  $(0, 0, 1)$  (click the Z Normal button). Having generated the cutting plane, the contours can be created using by the Contour filter described in User Guide section 7.1.8.

#### <span id="page-24-0"></span>2.1.4.2 Vector plots

Before we start to plot the vectors of the flow velocity, it may be useful to remove other modules that have been created, e.g. using the Slice and Contour filters described above. These can: either be deleted entirely, by highlighting the relevant module in the Pipeline Browser and clicking Delete in their respective Properties panel; or, be disabled by toggling the eye button for the relevant module in the Pipeline Browser.

We now wish to generate a vector glyph for velocity at the centre of each cell. We first need to filter the data to cell centres as described in User Guide section 7.1.9.1. With the cavity.OpenFOAM module highlighted in the Pipeline Browser, the user should select Cell Centers from the Filter->Alphabetical menu and then click Apply.

With these Centers highlighted in the Pipeline Browser, the user should then select Glyph from the Filter->Alphabetical menu. The Properties window panel should appear as shown in Figure [2.6.](#page-25-0) In the resulting Properties panel, the velocity field, U, is automatically selected in the vectors menu, since it is the only vector field present. By default the Scale Mode for the glyphs will be Vector Magnitude of velocity but, since the we may wish to view the velocities throughout the domain, the user should instead select off and Set Scale Factor to 0.005. On clicking Apply, the glyphs appear coloured by pressure. The user should also select Show Color Legend in Edit Color Map. The output is shown in Figure [2.7,](#page-25-1) in which uppercase Times Roman fonts are selected for the Color Legend headings and the labels are specified to 2 fixed significant figures by deselecting Automatic Label Format and entering %-#6.2f in the Label Format text box. The background colour is set to white in the Properties as described in User Guide section 7.1.7.1.

Note that at the left and right walls, glyphs appear to indicate flow through the walls. On closer examination, however, the user can see that while the flow direction is normal to the wall, its magnitude is 0. This slightly confusing situation is caused by ParaView choosing to orientate the glyphs in the x-direction when the glyph scaling off and the velocity magnitude is 0.





<span id="page-25-0"></span>Figure 2.6: Properties panel for the Glyph filter.



<span id="page-25-1"></span>Figure 2.7: Velocities in the cavity case.

<span id="page-26-0"></span>

#### <span id="page-27-0"></span>2.1.4.3 Streamline plots

Again, before the user continues to post-process in ParaView, they should disable modules such as those for the vector plot described above. We now wish to plot streamlines of velocity as described in User Guide section 7.1.10.

With the cavity. OpenFOAM module highlighted in the Pipeline Browser, the user should then select Stream Tracer from the Filter menu and then click Apply. The Properties window panel should appear as shown in Figure [2.8.](#page-26-0) The Seed points should be specified along a Line Source running vertically through the centre of the geometry, *i.e.* from  $(0.05, 0, 0.005)$  to  $(0.05, 0.1, 0.005)$ . For the image in this guide we used: a point Resolution of 21; Max Propagation by Length 0.5; Initial Step Length by Cell Length 0.01; and, Integration Direction BOTH. The Runge-Kutta 2 IntegratorType was used with default parameters.

On clicking Apply the tracer is generated. The user should then select Tube from the Filter menu to produce high quality streamline images. For the image in this report, we used: Num. sides 6; Radius 0.0003; and, Radius factor 10. The streamtubes are coloured by velocity magnitude. On clicking Apply the image in Figure [2.9](#page-41-0) should be produced.

## <span id="page-27-1"></span>2.1.5 Increasing the mesh resolution

The mesh resolution will now be increased by a factor of two in each direction. The results from the coarser mesh will be mapped onto the finer mesh to use as initial conditions for the problem. The solution from the finer mesh will then be compared with those from the coarser mesh.

#### <span id="page-27-2"></span>2.1.5.1 Creating a new case using an existing case

We now wish to create a new case named cavityFine that is created from cavity. The user should therefore clone the cavity case and edit the necessary files. First the user should create a new case directory at the same directory level as the cavity case, e.g.

#### cd \$FOAM RUN/tutorials/incompressible/icoFoam/cavity mkdir cavityFine

The user should then copy the base directories from the cavity case into cavityFine, and then enter the cavityFine case.

```
cp -r cavity/constant cavityFine
cp -r cavity/system cavityFine
cd cavityFine
```
## <span id="page-27-3"></span>2.1.5.2 Creating the finer mesh

We now wish to increase the number of cells in the mesh by using blockMesh. The user should open the **blockMeshDict** file in an editor and edit the block specification. The blocks are specified in a list under the blocks keyword. The syntax of the block definitions is described fully in User Guide section 4.3.1.3; at this stage it is sufficient to know that following hex is first the list of vertices in the block, then a list (or vector) of numbers of cells in each direction. This was originally set to (20 20 1) for the cavity case. The user should now change this to (40 40 1) and save the file. The new refined mesh should then be created by running blockMesh as before.

## <span id="page-28-0"></span>2.1.5.3 Mapping the coarse mesh results onto the fine mesh

The mapFields utility maps one or more fields relating to a given geometry onto the corresponding fields for another geometry. In our example, the fields are deemed 'consistent' because the geometry and the boundary types, or conditions, of both source and target fields are identical. We use the -consistent command line option when executing mapFields in this example.

The field data that mapFields maps is read from the time directory specified by startFrom/startTime in the controlDict of the target case, i.e. those into which the results are being mapped. In this example, we wish to map the final results of the coarser mesh from case cavity onto the finer mesh of case cavityFine. Therefore, since these results are stored in the 0.5 directory of cavity, the startTime should be set to 0.5 s in the controlDict dictionary and startFrom should be set to startTime.

The case is ready to run mapFields. Typing mapFields -help quickly shows that map-Fields requires the source case directory as an argument. We are using the -consistent option, so the utility is executed from within the cavityFine directory by

mapFields ../cavity -consistent

The utility should run with output to the terminal including:

```
Source: ".." "cavity"
Target: "." "cavityFine"
Create databases as time
Source time: 0.5
Target time: 0.5
Create meshes
Source mesh size: 400 Target mesh size: 1600
Consistently creating and mapping fields for time 0.5
    interpolating p
    interpolating U
End
```
## <span id="page-28-1"></span>2.1.5.4 Control adjustments

To maintain a Courant number of less that 1, as discussed in section [2.1.1.4,](#page-19-0) the time step must now be halved since the size of all cells has halved. Therefore deltaT should be set to to 0.0025 s in the controlDict dictionary. Field data is currently written out at an interval of a fixed number of time steps. Here we demonstrate how to specify data output at fixed intervals of time. Under the writeControl keyword in controlDict, instead of requesting output by a fixed number of time steps with the timeStep entry, a fixed amount of run time can be specified between the writing of results using the runTime entry. In this case the user should specify output every 0.1 and therefore should set writeInterval to 0.1 and writeControl to runTime. Finally, since the case is starting with a the solution obtained on the coarse mesh we only need to run it for a short period to achieve reasonable convergence to steady-state. Therefore the endTime should be set to 0.7 s. Make sure these settings are correct and then save the file.

## <span id="page-28-2"></span>2.1.5.5 Running the code as a background process

The user should experience running icoFoam as a background process, redirecting the terminal output to a log file that can be viewed later. From the cavityFine directory, the user should execute:

```
icoFoam > log &
cat log
```
### <span id="page-29-0"></span>2.1.5.6 Vector plot with the refined mesh

The user can open multiple cases simultaneously in ParaView; essentially because each new case is simply another module that appears in the Pipeline Browser. There is one minor inconvenience when opening a new case in ParaView because there is a prerequisite that the selected data is a file with a name that has an extension. However, in OpenFOAM, each case is stored in a multitude of files with no extensions within a specific directory structure. The solution, that the paraFoam script performs automatically, is to create a dummy file with the extension  $\mathcal{O}penFOAM$  — hence, the cavity case module is called cavity.OpenFOAM.

However, if the user wishes to open another case directly from within ParaView, they need to create such a dummy file. For example, to load the cavityFine case the file would be created by typing at the command prompt:

#### cd \$FOAM RUN/tutorials/incompressible/icoFoam/cavity touch cavityFine/cavityFine.OpenFOAM

Now the cavityFine case can be loaded into ParaView by selecting Open from the File menu, and having navigated the directory tree, selecting cavityFine. OpenFOAM. The user can now make a vector plot of the results from the refined mesh in ParaView. The plot can be compared with the cavity case by enabling glyph images for both case simultaneously.

## <span id="page-29-1"></span>2.1.5.7 Plotting graphs

The user may wish to visualise the results by extracting some scalar measure of velocity and plotting 2-dimensional graphs along lines through the domain. OpenFOAM is well equipped for this kind of data manipulation. There are numerous utilities that perform specialised data manipulations, and many can be accessed via the postProcess utility:

```
postProcess -list
```
returns the list:

```
CourantNo
Lambda2
MachNo
PecletNo
\OmegaR
XiReactionRate
add
boundaryCloud
cellMax
cellMin
components
div
enstrophy
```
faceMax faceMin flowRatePatch flowType forceCoeffsCompressible forceCoeffsIncompressible forcesCompressible forcesIncompressible grad internalCloud mag magSqr minMaxComponents minMaxMagnitude patchAverage patchIntegrate pressureDifferencePatch pressureDifferenceSurface probes randomise residuals scalarTransport singleGraph staticPressure streamFunction streamlines subtract surfaces totalPressureCompressible totalPressureIncompressible turbulenceFields volFlowRateSurface vorticity wallHeatFlux wallShearStress writeCellCentres writeCellVolumes writeObjects yPlus

The components and mag functions provide useful scalar measures of velocity.

When the components function is run on a case, say *cavity*, it reads the velocity vector field from each time directory and, in the corresponding time directories, writes scalar fields Ux, Uy and Uz representing the  $x, y$  and  $z$  components of velocity. Similarly the mag function writes a scalar field magU to each time directory representing the magnitude of velocity.

The user can run both functions simultaneously,  $e.g.$  for the cavity case the user should go into the cavity directory and execute postProcess as follows:

```
cd $FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavity
postProcess -funcs '(components(U) mag(U))'
```
The individual components can be plotted as a graph in ParaView. It is quick, convenient and has reasonably good control over labelling and formatting, so the printed output is a fairly good standard. However, to produce graphs for publication, users may prefer to write raw data and plot it with a dedicated graphing tool, such as gnuplot or Grace/xmgr. To do this, see section [5.1.4.](#page-97-0)

Before commencing plotting, the user needs to load the newly generated Ux, Uy and Uz fields into ParaView. To do this, the user should click the Refresh button at the top of the Properties panel for the cavity.OpenFOAM module which will cause the new fields to be loaded into ParaView and appear in the Volume Fields window. Ensure the new fields are selected and the changes are applied, i.e. click Apply again if necessary. Also, data is interpolated incorrectly at boundaries if the boundary regions are selected in the Mesh Parts panel. Therefore the user should *deselect the patches* in the Mesh Parts panel, i.e.movingWall, fixedWall and frontAndBack, and apply the changes.

Now, in order to display a graph in ParaView the user should select the module of interest, e.g.cavity.OpenFOAM and apply the Plot Over Line filter from the Filter->Data Analysis menu. This opens up a new XY Plot window below or beside the existing 3D View window. A PlotOverLine module is created in which the user can specify the end points of the line in the Properties panel. In this example, the user should position the line vertically up the centre of the domain, *i.e.* from  $(0.05, 0, 0.005)$  to  $(0.05, 0.1, 0.005)$ , in the Point1 and Point2 text boxes. The Resolution can be set to 100.

On clicking Apply, a graph is generated in the XY Plot window. In the Display panel, the Attribute Mode is set to Point Data by default. The Use Data Array option can be selected for the X Axis Data, taking the arc length option so that the x-axis of the graph represents distance from the base of the cavity.

The user can choose the fields to be displayed in the Line Series panel of the Display window. From the list of scalar fields to be displayed, it can be seen that the magnitude and components of vector fields are available by default, e.g. displayed as U:X, so that it was not necessary to create Ux using **postProcess**. Nevertheless, the user should deselect all series except  $Ux$  (or  $U:x$ ). A square colour box in the adjacent column to the selected series indicates the line colour. The user can edit this most easily by a double click of the mouse over that selection.

In order to format the graph, the user should modify the settings below the Line Series panel, namely Line Color, Line Thickness, Line Style, Marker Style and Chart Axes.

Also the user can click one of the buttons above the top left corner of the XY Plot. The third button, for example, allows the user to control View Settings in which the user can set title and legend for each axis, for example. Also, the user can set font, colour and alignment of the axes titles, and has several options for axis range and labels in linear or logarithmic scales.

Figure [2.11](#page-42-0) is a graph produced using ParaView. The user can produce a graph however he/she wishes. For information, the graph in Figure [2.11](#page-42-0) was produced with the options for axes of: Standard type of Notation; Specify Axis Range selected; titles in Sans Serif 12 font. The graph is displayed as a set of points rather than a line by activating the Enable Line Series button in the Display window. Note: if this button appears to be inactive by being "greyed out", it can be made active by selecting and deselecting the sets of variables in the Line Series panel. Once the Enable Line Series button is selected, the Line Style and Marker Style can be adjusted to the user's preference.

## <span id="page-32-0"></span>2.1.6 Introducing mesh grading

The error in any solution will be more pronounced in regions where the form of the true solution differ widely from the form assumed in the chosen numerical schemes. For example a numerical scheme based on linear variations of variables over cells can only generate an exact solution if the true solution is itself linear in form. The error is largest in regions where the true solution deviates greatest from linear form, i.e. where the change in gradient is largest. Error decreases with cell size.

It is useful to have an intuitive appreciation of the form of the solution before setting up any problem. It is then possible to anticipate where the errors will be largest and to grade the mesh so that the smallest cells are in these regions. In the cavity case the large variations in velocity can be expected near a wall and so in this part of the tutorial the mesh will be graded to be smaller in this region. By using the same number of cells, greater accuracy can be achieved without a significant increase in computational cost.

A mesh of  $20 \times 20$  cells with grading towards the walls will be created for the lid-driven cavity problem and the results from the finer mesh of section [2.1.5.2](#page-27-3) will then be mapped onto the graded mesh to use as an initial condition. The results from the graded mesh will be compared with those from the previous meshes. Since the changes to the **blockMeshDict** dictionary are fairly substantial, the case used for this part of the tutorial, cavityGrade, is supplied in the **\$FOAM\_RUN/tutorials/incompressible/icoFoam/cavity** directory.

#### <span id="page-32-1"></span>2.1.6.1 Creating the graded mesh

The mesh now needs 4 blocks as different mesh grading is needed on the left and right and top and bottom of the domain. The block structure for this mesh is shown in Figure [2.12.](#page-42-1) The user can view the *blockMeshDict* file in the *system* subdirectory of cavityGrade; for completeness the key elements of the **blockMeshDict** file are also reproduced below. Each block now has 10 cells in the  $x$  and  $y$  directions and the ratio between largest and smallest cells is 2.

```
17 scale 0.1;
18
19 vertices
\frac{20}{21}\begin{array}{c} 21 \\ 22 \end{array} (0 0 0)<br>
\begin{array}{c} (0.5 \ 0) \end{array}22 (0.5 \ 0 \ 0)23 (1 0 0)
24 (0 0.5 0)
25 (0.5 \ 0.5 \ 0)26 (1 0.5 0)
27 (0 1 0)
28 (0.5 1 0)
29 (1 1 0)
30 (0 0 0.1)
31 \hspace{1.5cm} (0.5 \hspace{1.5cm} 0 \hspace{1.5cm} 0.1)32 (1 0 0.1)
33 (0 0.5 0.1)
34 (0.5 0.5 0.1)
35 \qquad (1 \; 0.5 \; 0.1)36 (0 1 0.1)
37 (0.5 1 0.1)
\begin{array}{c} 37 \\ 38 \\ 39 \end{array} (1 1 0.1)
     ) ;
40
41 blocks
rac{42}{43}hex (0 1 4 3 9 10 13 12) (10 10 1) simpleGrading (2 2 1)
44 hex (1 2 5 4 10 11 14 13) (10 10 1) simpleGrading (0.5 2 1)
45 hex (3 4 7 6 12 13 16 15) (10 10 1) simpleGrading (2 0.5 1)
46 hex (4 5 8 7 13 14 17 16) (10 10 1) simpleGrading (0.5 0.5 1)
47 );
48
49 edges
\begin{matrix} 50 & 0 \\ 51 & 0 \end{matrix}\mathcal{E}:52
53 boundary
```


Once familiar with the *blockMeshDict* file for this case, the user can execute blockMesh from the command line. The graded mesh can be viewed as before using paraFoam as described in section [2.1.2.](#page-20-1)

## <span id="page-33-0"></span>2.1.6.2 Changing time and time step

The highest velocities and smallest cells are next to the lid, therefore the highest Courant number will be generated next to the lid, for reasons given in section [2.1.1.4.](#page-19-0) It is therefore useful to estimate the size of the cells next to the lid to calculate an appropriate time step for this case.

When a nonuniform mesh grading is used, blockMesh calculates the cell sizes using a geometric progression. Along a length  $l$ , if  $n$  cells are requested with a ratio of  $R$  between the last and first cells, the size of the smallest cell,  $\delta x_s$ , is given by:

$$
\delta x_s = l \frac{r-1}{\alpha r - 1} \tag{2.5}
$$

where  $r$  is the ratio between one cell size and the next which is given by:

$$
r = R^{\frac{1}{n-1}}\tag{2.6}
$$

and

$$
\alpha = \begin{cases} R & \text{for } R > 1, \\ 1 - r^{-n} + r^{-1} & \text{for } R < 1. \end{cases}
$$
 (2.7)

For the cavityGrade case the number of cells in each direction in a block is 10, the ratio between largest and smallest cells is 2 and the block height and width is 0.05 m. Therefore the smallest cell length is 3.45 mm. From Equation [2.2,](#page-19-1) the time step should be less than 3.45 ms to maintain a Courant of less than 1. To ensure that results are written out at convenient time intervals, the time step deltaT should be reduced to 2.5 ms and the writeInterval set to 40 so that results are written out every 0.1 s. These settings can be viewed in the cavityGrade/system/controlDict file.

The startTime needs to be set to that of the final conditions of the case cavityFine, *i.e.*0.7. Since cavity and cavity Fine converged well within the prescribed run time, we can set the run time for case cavityGrade to 0.1 s, *i.e.* the endTime should be 0.8.

## <span id="page-34-0"></span>2.1.6.3 Mapping fields

As in section [2.1.5.3,](#page-28-0) use mapFields to map the final results from case cavityFine onto the mesh for case cavityGrade. Enter the *cavityGrade* directory and execute mapFields by:

cd \$FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavityGrade mapFields ../cavityFine -consistent

Now run icoFoam from the case directory and monitor the run time information. View the converged results for this case and compare with other results using post-processing tools described previously in section [2.1.5.6](#page-29-0) and section [2.1.5.7.](#page-29-1)

## <span id="page-34-1"></span>2.1.7 Increasing the Reynolds number

The cases solved so far have had a Reynolds number of 10. This is very low and leads to a stable solution quickly with only small secondary vortices at the bottom corners of the cavity. We will now increase the Reynolds number to 100, at which point the solution takes a noticeably longer time to converge. The coarsest mesh in case cavity will be used initially. The user should make a copy of the cavity case and name it cavityHighRe by typing:

```
cd $FOAM_RUN/tutorials/incompressible/icoFoam/cavity
cp -r cavity cavityHighRe
```
## <span id="page-34-2"></span>2.1.7.1 Pre-processing

Enter the cavityHighRe case and edit the transportProperties dictionary. Since the Reynolds number is required to be increased by a factor of 10, decrease the kinematic viscosity by a factor of 10, *i.e.* to  $1 \times 10^{-3}$  m<sup>2</sup>s<sup>-1</sup>. We can now run this case by restarting from the solution at the end of the cavity case run. To do this we can use the option of setting the startFrom keyword to latestTime so that icoFoam takes as its initial data the values stored in the directory corresponding to the most recent time, i.e. 0.5. The endTime should be set to 2 s.

## <span id="page-34-3"></span>2.1.7.2 Running the code

Run icoFoam for this case from the case directory and view the run time information. When running a job in the background, the following UNIX commands can be useful:

nohup enables a command to keep running after the user who issues the command has logged out;

nice changes the priority of the job in the kernel's scheduler; a niceness of -20 is the highest priority and 19 is the lowest priority.

This is useful, for example, if a user wishes to set a case running on a remote machine and does not wish to monitor it heavily, in which case they may wish to give it low priority on the machine. In that case the nohup command allows the user to log out of a remote machine he/she is running on and the job continues running, while nice can set the priority to 19. For our case of interest, we can execute the command in this manner as follows:

```
cd $FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavityHighRe
nohup nice -n 19 icoFoam > log &
cat log
```
In previous runs you may have noticed that icoFoam stops solving for velocity U quite quickly but continues solving for pressure p for a lot longer or until the end of the run. In practice, once icoFoam stops solving for U and the initial residual of p is less than the tolerance set in the fvSolution dictionary (typically  $10^{-6}$ ), the run has effectively converged and can be stopped once the field data has been written out to a time directory. For example, at convergence a sample of the *log* file from the run on the cavity HighRe case appears as follows in which the velocity has already converged after 1.62 s and initial pressure residuals are small; No Iterations 0 indicates that the solution of U has stopped:

```
Time = 1.633
 <sub>3</sub><br>4 Courant Number mean: 0.221985 max: 0.839923<br>5 smoothSolver: Solving for Ux. Initial resid
  5 smoothSolver: Solving for Ux, Initial residual = 3.64032e-06, Final residual = 3.64032e-06, No Iterations 0
6 smoothSolver: Solving for Uy, Initial residual = 4.20677e-06, Final residual = 4.20677e-06, No Iterations 0
DICPCG: Solving for p, Initial residual = 2.11678e-06, Final residual = 7.25303e-07, No Iterations 3<br>
8 time step continuity errors : sum local = 7.25166e-09, global = 4.96308e-19, cumulative = -1.28342e-17<br>
9 DICPCG: Solv
\begin{array}{c} 12 \\ 13 \end{array}Time = 1.635\frac{14}{15}Courant Number mean: 0.221986 max: 0.839923<br>
16 smoothSolver: Solving for Ux, Initial residual = 3.56036e-06, Final residual = 3.56036e-06, No Iterations 0<br>
17 smoothSolver: Solving for Uy, Initial residual = 4.11726e-06, 
21 time step continuity errors : sum local = 8.25673e-09, global = 5.87298e-20, cumulative = -1.38816e-17
22 ExecutionTime = 0.38 s ClockTime = 0 s
```
## <span id="page-35-0"></span>2.1.8 High Reynolds number flow

View the results in paraFoam and display the velocity vectors. The secondary vortices in the corners have increased in size somewhat. The user can then increase the Reynolds number further by decreasing the viscosity and then rerun the case. The number of vortices increases so the mesh resolution around them will need to increase in order to resolve the more complicated flow patterns. In addition, as the Reynolds number increases the time to convergence increases. The user should monitor residuals and extend the endTime accordingly to ensure convergence.

The need to increase spatial and temporal resolution then becomes impractical as the flow moves into the turbulent regime, where problems of solution stability may also occur. Of course, many engineering problems have very high Reynolds numbers and it is infeasible to bear the huge cost of solving the turbulent behaviour directly. Instead Reynolds-averaged simulation (RAS) turbulence models are used to solve for the mean flow behaviour and calculate the statistics of the fluctuations. The standard  $k - \varepsilon$  model with wall functions will be used in this tutorial to solve the lid-driven cavity case with

1
a Reynolds number of  $10^4$ . Two extra variables are solved for:  $k$ , the turbulent kinetic energy; and,  $\varepsilon$ , the turbulent dissipation rate. The additional equations and models for turbulent flow are implemented into a OpenFOAM solver called pisoFoam.

#### <span id="page-36-0"></span>2.1.8.1 Pre-processing

17

Change directory to the cavity case in the \$FOAM RUN/tutorials/incompressible/pisoFoam/- RAS directory (N.B: the **pisoFoam/RAS** directory). Generate the mesh by running blockMesh as before. Mesh grading towards the wall is not necessary when using the standard  $k - \varepsilon$  model with wall functions since the flow in the near wall cell is modelled, rather than having to be resolved.

A range of wall function models is available in OpenFOAM that are applied as boundary conditions on individual patches. This enables different wall function models to be applied to different wall regions. The choice of wall function models are specified through the turbulent viscosity field,  $\nu_t$  in the  $0/$ *nut* file:

```
18 dimensions [0 2 -1 0 0 0 0];19
20 internalField uniform 0;
21
22 boundaryField
\frac{23}{24}movingWall
\frac{25}{26} {
26 type nutkWallFunction;<br>27 value uniform 0:
\begin{array}{ccc} 27 & & \text{value} \\ 28 & & \end{array} uniform 0;
28 }
29 fixedWalls
30 {
31 type nutkWallFunction;<br>32 value uniform 0:
\begin{array}{ccc}\n 32 \\
 33\n \end{array} value uniform 0;
33 }
34 frontAndBack
35 {
36 type empty;<br>37 }
37 }
\frac{3}{38} }
39
40
41 // ************************************************************************* //
```
This case uses standard wall functions, specified by the nutWallFunction keyword entry on the movingWall and fixedWalls patches. Other wall function models include the rough wall functions, specified though the nutRoughWallFunction keyword.

The user should now open the field files for k and  $\varepsilon$  ( $0/k$  and  $0/epsilon$ ) and examine their boundary conditions. For a wall boundary condition wall,  $\varepsilon$  is assigned a epsilon-WallFunction boundary condition and a kqRwallFunction boundary condition is assigned to k. The latter is a generic boundary condition that can be applied to any field that are of a turbulent kinetic energy type, e.g. k, q or Reynolds Stress  $R$ . The initial values for k and  $\varepsilon$  are set using an estimated fluctuating component of velocity U' and a turbulent length scale, l. k and  $\varepsilon$  are defined in terms of these parameters as follows:

$$
k = \frac{1}{2}\overline{\mathbf{U}' \cdot \mathbf{U}'} \tag{2.8}
$$

$$
\varepsilon = \frac{C_{\mu}^{0.75} k^{1.5}}{l} \tag{2.9}
$$

where  $C_{\mu}$  is a constant of the  $k - \varepsilon$  model equal to 0.09. For a Cartesian coordinate system,  $k$  is given by:

$$
k = \frac{1}{2}(U_x'^2 + U_y'^2 + U_z'^2) \tag{2.10}
$$

where  $U'_x{}^2$  $\frac{y}{x}$ ,  $U'_y$  2  $y^{\prime 2}$  and  $U_{z}^{\prime 2}$  $z^2$  are the fluctuating components of velocity in the x, y and z directions respectively. Let us assume the initial turbulence is isotropic, *i.e.*  $U'_x{}^2 = U'_y{}^2 =$  $U_z^{\prime}$ <sup>2</sup>  $\mathbb{Z}_z^2$ , and equal to 5% of the lid velocity and that l, is equal to 20% of the box width, 0.1 m, then k and  $\varepsilon$  are given by:

$$
U_x' = U_y' = U_z' = \frac{5}{100} 1 \text{ m s}^{-1}
$$
\n(2.11)

$$
\Rightarrow k = \frac{3}{2} \left( \frac{5}{100} \right)^2 \, \text{m}^2 \, \text{s}^{-2} = 3.75 \times 10^{-3} \, \text{m}^2 \, \text{s}^{-2} \tag{2.12}
$$

$$
\varepsilon = \frac{0.09^{0.75} \times (3.75 \times 10^{-3})^{1.5}}{0.2 \times 0.1} \approx 1.89 \times 10^{-3} \text{ m}^2 \text{s}^{-3}
$$
 (2.13)

These form the initial conditions for k and  $\varepsilon$ . The initial conditions for U and p are  $(0, 0, 0)$  and 0 respectively as before.

Turbulence modelling includes a range of methods, e.g. RAS or large-eddy simulation (LES), that are provided in OpenFOAM. In most transient solvers, the choice of turbulence modelling method is selectable at run-time through the simulationType keyword in *turbulenceProperties* dictionary. The user can view this file in the *constant* directory:

```
17
18 simulationType RAS;
19
\begin{matrix} 20 & \text{RAS} \\ 21 & \text{f} \end{matrix}21 {
22 RASModel kEpsilon;
23
<sup>24</sup> turbulence on;
25
26 printCoeffs on;<br>27 }
27 }
28
29 // ************************************************************************* //
```
The options for simulationType are laminar, RAS and LES. More informaton on turbulence models can be found in the [Extended Code Guide](http://openfoam.com/documentation/cpp-guide/html/guide-turbulence.html) With RAS selected in this case, the choice of RAS modelling is specified in a turbulenceProperties subdictionary, also in the constant directory. The turbulence model is selected by the RASModel entry from a long list of available models that are listed in User Guide Table A.5. The kEpsilon model should be selected which is is the standard  $k - \varepsilon$  model; the user should also ensure that turbulence calculation is switched on.

The coefficients for each turbulence model are stored within the respective code with a set of default values. Setting the optional switch called printCoeffs to on will make the default values be printed to standard output, i.e. the terminal, when the model is called at run time. The coefficients are printed out as a sub-dictionary whose name is that of the model name with the word Coeffs appended,  $e.q.$  kEpsilonCoeffs in the case of the kEpsilon model. The coefficients of the model, e.g. kEpsilon, can be modified by optionally including (copying and pasting) that sub-dictionary within the turbulenceProperties file and adjusting values accordingly.

The user should next set the laminar kinematic viscosity in the *transportProperties* dictionary. To achieve a Reynolds number of  $10^4$ , a kinematic viscosity of  $10^{-5}$  m is required based on the Reynolds number definition given in Equation [2.1.](#page-18-0)

Finally the user should set the startTime, stopTime, deltaT and the writeInterval in the controlDict. Set deltaT to 0.005 s to satisfy the Courant number restriction and the endTime to 10 s.

#### 2.1.8.2 Running the code

Execute pisoFoam by entering the case directory and typing "pisoFoam" in a terminal. In this case, where the viscosity is low, the boundary layer next to the moving lid is

very thin and the cells next to the lid are comparatively large so the velocity at their centres are much less than the lid velocity. In fact, after  $\approx 100$  time steps it becomes apparent that the velocity in the cells adjacent to the lid reaches an upper limit of around  $0.2 \text{ m s}^{-1}$  hence the maximum Courant number does not rise much above 0.2. It is sensible to increase the solution time by increasing the time step to a level where the Courant number is much closer to 1. Therefore reset deltaT to 0.02 s and, on this occasion, set startFrom to latestTime. This instructs pisoFoam to read the start data from the latest time directory, *i.e.*10.0. The endTime should be set to 20 s since the run converges a lot slower than the laminar case. Restart the run as before and monitor the convergence of the solution. View the results at consecutive time steps as the solution progresses to see if the solution converges to a steady-state or perhaps reaches some periodically oscillating state. In the latter case, convergence may never occur but this does not mean the results are inaccurate.

## 2.1.9 Changing the case geometry

A user may wish to make changes to the geometry of a case and perform a new simulation. It may be useful to retain some or all of the original solution as the starting conditions for the new simulation. This is a little complex because the fields of the original solution are not consistent with the fields of the new case. However the mapFields utility can map fields that are inconsistent, either in terms of geometry or boundary types or both.

As an example, let us go to the cavityClipped case in the *icoFoam* directory which consists of the standard cavity geometry but with a square of length 0.04 m removed from the bottom right of the cavity, according to the blockMeshDict below:

```
17 scale 0.1;
18
19 vertices
\frac{20}{21}21 (0 0 0)
22 (0.6 0 0)
\begin{array}{c}\n 23 \\
 24\n \end{array}
(0 0.4 0)
\begin{array}{cc} 24 & (0.6 \ 0.4 \ 0) \\ 25 & (1 \ 0.4 \ 0) \end{array}25 (1 0.4 0)
26 (0 1 0)
\begin{array}{cc} 27 & \text{(0.6 1 0)} \\ 28 & \text{(1 1 0)} \end{array}(1 \; 1 \; 0)29
30 (0 0 0.1)
31 (0.6 0 0.1)
32 (0 0.4 0.1)
\begin{array}{cc}\n 33 \\
 34\n \end{array}
(0.6 \ 0.4 \ 0.1)34 (1 0.4 0.1)
35 (0 1 0.1)
36 (0.6 1 0.1)
37 (1 1 0.1)
38
\frac{39}{39} );
40
41 blocks
\frac{42}{43}hex (0 1 3 2 8 9 11 10) (12 8 1) simpleGrading (1 1 1)
44 hex (2 3 6 5 10 11 14 13) (12 12 1) simpleGrading (1 1 1)
45 hex (3 4 7 6 11 12 15 14) (8 12 1) simpleGrading (1 1 1)
46 );
47
48 edges
49 (
50 );
51
52 boundary
\begin{array}{c} 53 \\ 54 \end{array} (
54 lid
55 {
56 type wall;<br>57 faces
57 faces
58 (
59 (5 13 14 6)
\begin{pmatrix} 6 & 14 & 15 & 7 \end{pmatrix}
```

```
61 );
62<br>63
\begin{array}{ccc}\n 63 & & \text{fixedWalls} \\
 64 & & \text{f}\n \end{array}64 {
65 type wall;
66 faces
67 (
68 (0 8 10 2)
69 (2 10 13 5)
70 (7 15 12 4)
71 (4 12 11 3)
\begin{array}{cc}\n 72 \\
 73 \\
 \hline\n 73\n \end{array}\n \qquad\n \begin{array}{cc}\n 3 & 11 & 9 & 1 \\
 1 & 9 & 8 & 0\n \end{array}\n \qquad\n \begin{array}{cc}\n 3 & 11 & 9 & 1 \\
 1 & 9 & 8 & 0\n \end{array}\n \qquad\n \begin{array}{cc}\n 3 & 11 & 9 & 1 \\
 1 & 9 & 8 & 0\n \end{array}\n \qquad\n \begin{array}{cc}\n 3 & 11 & 9 & 1 \\
 1 & 9 & 8 & 0\n \end{array}\n \qquad\n \begin{array}{cc}\n 3 & 11(1 9 8 0)\frac{74}{75} );
75 }
76 frontAndBack
77 {
78 type empty;
79 faces
80 (
\begin{array}{c} 81 \\ 82 \\ 83 \end{array}
(0 2 3 1)<br>
(2 5 6 3)<br>
(3 6 7 4)
82 (2 5 6 3)
83 (3 6 7 4)
84 (8 9 11 10)
85 (10 11 14 13)
86 (11 12 15 14)
\begin{array}{ccc} 87 & & \\ 88 & & \\ \end{array} );
88 }
\overline{89} );
90
91 mergePatchPairs
92 (
93 );
94
95 // ************************************************************************* //
```
Generate the mesh with blockMesh. The patches are set as according to the previous cavity cases. For the sake of clarity in describing the field mapping process, the upper wall patch is renamed lid, previously the moving Wall patch of the original cavity.

In an inconsistent mapping, there is no guarantee that all the field data can be mapped from the source case. The remaining data must come from field files in the target case itself. Therefore field data must exist in the time directory of the target case before mapping takes place. In the cavityClipped case the mapping is set to occur at time 0.5 s, since the startTime is set to 0.5 s in the *controlDict*. Therefore the user needs to copy initial field data to that directory, e.g. from time 0:

```
cd $FOAM RUN/tutorials/incompressible/icoFoam/cavity/cavityClipped
cp -r 0 0.5
```
Before mapping the data, the user should view the geometry and fields at 0.5 s.

Now we wish to map the velocity and pressure fields from cavity onto the new fields of cavityClipped. Since the mapping is inconsistent, we need to edit the mapFieldsDict dictionary, located in the **system** directory. The dictionary contains 2 keyword entries: patchMap and cuttingPatches. The patchMap list contains a mapping of patches from the source fields to the target fields. It is used if the user wishes a patch in the target field to inherit values from a corresponding patch in the source field. In cavityClipped, we wish to inherit the boundary values on the lid patch from moving Wall in cavity so we must set the patchMap as:

```
patchMap
(
    lid movingWall
);
```
The cuttingPatches list contains names of target patches whose values are to be mapped from the source internal field through which the target patch cuts. In this case we will include the fixedWalls to demonstrate the interpolation process.

```
cuttingPatches
(
    fixedWalls
);
```
Now the user should run mapFields, from within the *cavityClipped* directory:

mapFields ../cavity

The user can view the mapped field as shown in Figure [2.13.](#page-42-0) The boundary patches have inherited values from the source case as we expected. Having demonstrated this, however, we actually wish to reset the velocity on the **fixedWalls** patch to  $(0, 0, 0)$ . Edit the U field, go to the fixedWalls patch and change the field from nonuniform to uniform  $(0, 0, 0)$ . The nonuniform field is a list of values that requires deleting in its entirety. Now run the case with icoFoam.

# 2.1.10 Post-processing the modified geometry

Velocity glyphs can be generated for the case as normal, first at time 0.5 s and later at time 0.6 s, to compare the initial and final solutions. In addition, we provide an outline of the geometry which requires some care to generate for a 2D case. The user should select Extract Block from the Filter menu and, in the Parameter panel, highlight the patches of interest, namely the lid and fixedWalls. On clicking Apply, these items of geometry can be displayed by selecting Wireframe in the Properties panel. Figure [2.14](#page-43-0) displays the patches in black and shows vortices forming in the bottom corners of the modified geometry.



Figure 2.9: Streamlines in the cavity case.



Figure 2.10: Selecting fields for graph plotting.



Figure 2.11: Plotting graphs in ParaView.



Figure 2.12: Block structure of the graded mesh for the cavity (block numbers encircled).



<span id="page-42-0"></span>Figure 2.13: cavity solution velocity field mapped onto cavityClipped.



<span id="page-43-0"></span>Figure 2.14: cavityClipped solution for velocity field.

# 2.2 Flow around a cylinder

Tutorial path:

• \$FOAM\_[TUTORIALS/basic/potentialFoam/cylinder](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/basic/potentialFoam/cylinder)

In this example we shall investigate potential flow around a cylinder using thepotentialFoam solver. This example introduces the following OpenFOAM features:

- non-orthogonal meshes;
- generating an analytical solution to a problem in OpenFOAM;
- use of a dynamic code to generate the block vertices;
- use of a coded function object to compare results against the analytical solution.

# 2.2.1 Problem specification

The problem is defined as follows:

**Solution domain** The domain is 2 dimensional and consists of a square domain with a cylinder collocated with the centre of the square as shown in Figure [2.15.](#page-44-0)



<span id="page-44-0"></span>Figure 2.15: Geometry of flow round a cylinder

# Governing equations

• Mass continuity for an incompressible fluid

$$
\nabla \cdot \mathbf{U} = 0 \tag{2.14}
$$

• Pressure equation for an incompressible, irrotational fluid assuming steadystate conditions

$$
\nabla^2 p = 0 \tag{2.15}
$$

#### Boundary conditions

- Inlet (left) with fixed velocity  $U = (1, 0, 0)$  m/s.
- Outlet (right) with a fixed pressure  $p = 0$  Pa.
- No-slip wall (bottom):
- Symmetry plane (top).
- **Initial conditions**  $U = 0$  m/s,  $p = 0$  Pa required in OpenFOAM input files but not necessary for the solution since the problem is steady-state.
- **Solver name potentialFoam:** a potential flow code, *i.e.* assumes the flow is incompressible, steady, irrotational, inviscid and it ignores gravity.
- Case name cylinder case located in the \$FOAM\_TUTORIALS/basic/potentialFoam directory.

# 2.2.2 Note on potentialFoam

potentialFoam is a useful solver to validate OpenFOAM since the assumptions of potential flow are such that an analytical solution exists for cases whose geometries are relatively simple. In this example of flow around a cylinder an analytical solution exists with which we can compare our numerical solution. potentialFoam can also be run more like a utility to provide a (reasonably) conservative initial U field for a problem. When running certain cases, this can useful for avoiding instabilities due to the initial field being unstable. In short, potentialFoam creates a conservative field from a non-conservative initial field supplied by the user.

# 2.2.3 Mesh generation

Mesh generation using blockMesh has been described in tutorials in the User Guide. In this case, the mesh consists of 10 blocks as shown in Figure [2.16.](#page-45-0) Remember that all



<span id="page-45-0"></span>Figure 2.16: Blocks in cylinder geometry

meshes are treated as 3 dimensional in OpenFOAM. If we wish to solve a 2 dimensional

problem, we must describe a 3 dimensional mesh that is only one cell thick in the third direction that is not solved. In Figure [2.16](#page-45-0) we show only the back plane of the geometry, along  $z = -0.5$ , in which the vertex numbers are numbered 0-18. The other 19 vertices in the front plane,  $z = +0.5$ , are numbered in the same order as the back plane, as shown in the mesh description file below:

```
1 /*--------------------------------*- C++ -*----------------------------------*\
 2 | ========= | |
3 | \\ / F ield | OpenFOAM: The Open Source CFD Toolbox |
4 | \\ / 0 peration | Version: v2006<br>
5 | \\ / A nd | Website: www.org
5 | \\ / A nd | Website: www.openfoam.com |
6 | \\/ M anipulation | |
7 \*---------------------------------------------------------------------------*/
    FoamFile
9 {
10 version 2.0;<br>11 format asci
11 format ascii;<br>
12 class dictio
        class dictionary<br>object blockMeshD
13 object blockMeshDict;
\frac{14}{15}15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 1;
18
19 vertices #codeStream
\frac{20}{21}\begin{array}{ccc} 21 & \text{codeIndie} \\ 22 & \text{tt} \end{array}\frac{22}{23} #
            #include "pointField.H"
24 #};
25
\frac{26}{27} code
        #28 pointField points(19);
29 points[0] = point(0.5, 0, -0.5);<br>30 points[1] = point(1, 0, -0.5);
30 points[1] = point(1, 0, -0.5);31 points[2] = point(2, 0, -0.5);<br>32 points[3] = point(2, 0.707107,
32 points[3] = point(2, 0.707107, -0.5);<br>33 points[4] = point(0.707107, 0.707107,
33 points[4] = point(0.707107, 0.707107, -0.5);
34 points[5] = point(0.353553, 0.353553, -0.5);
35 points[6] = point(2, 2, -0.5);<br>36 points[7] = point(0.707107, 2,
36 points[7] = point(0.707107, 2, -0.5);37 points[8] = point(0, 2, -0.5);
38 \t\t point 5[9] = point(0, 1, -0.5);39 points[10] = point(0, 0.5, -0.5);
40 points[11] = point(-0.5, 0, -0.5);41 		 points [12] = point(-1, 0, -0.5);42 		 points [13] = point(-2, 0, -0.5);43 		 points [14] = point(-2, 0.707107, -0.5);
44 points[15] = point(-0.707107, 0.707107, -0.5);
45 points[16] = point(-0.353553, 0.353553, -0.5);
46 points [17] = \frac{1}{2} point (-2, 2, -0.5);
47 		 points [18] = point(-0.707107, 2, -0.5);
48
49 // Duplicate z points
50 label sz = points.size();
51 points.setSize(2*sz);
52 for (label i = 0; i < sz; i++)<br>5353 {
54 const point & pt = points [i];
55 points[i+sz] = point(pt.x(), pt.y(), -pt.z());<br>56
56 }
57
58 os << points;
\begin{matrix}59 \\ 60 \end{matrix} \begin{matrix} \text{#} \\ \text{+} \end{matrix}60 };
61
62
63 blocks
64<br>65
        65 hex (5 4 9 10 24 23 28 29) (10 10 1) simpleGrading (1 1 1)
66 hex (0 1 4 5 19 20 23 24) (10 10 1) simpleGrading (1 1 1)
67 hex (1 2 3 4 20 21 22 23) (20 10 1) simpleGrading (1 1 1)
68 hex (4 3 6 7 23 22 25 26) (20 20 1) simpleGrading (1 1 1)
69 hex (9 4 7 8 28 23 26 27) (10 20 1) simpleGrading (1 1 1)
70 hex (15 16 10 9 34 35 29 28) (10 10 1) simpleGrading (1 1 1)
```

```
71 hex (12 11 16 15 31 30 35 34) (10 10 1) simpleGrading (1 1 1)
72 hex (13 12 15 14 32 31 34 33) (20 10 1) simpleGrading (1 1 1)
73 hex (14 15 18 17 33 34 37 36) (20 20 1) simpleGrading (1 1 1)
74 hex (15 9 8 18 34 28 27 37) (10 20 1) simpleGrading (1 1 1)
75 );
76
77 edges
\frac{78}{79} (
 79 arc 0 5 (0.469846 0.17101 -0.5)
 80 arc 5 10 (0.17101 0.469846 -0.5)
 81 arc 1 4 (0.939693 0.34202 -0.5)
 82 arc 4 9 (0.34202 0.939693 -0.5)
82 arc 4 9 (0.34202 0.939693 -0.5)<br>
83 arc 19 24 (0.469846 0.17101 0.5)<br>
84 arc 24 29 (0.17101 0.469846 0.5)<br>
85 arc 20 23 (0.939693 0.34202 0.5)<br>
86 arc 23 28 (0.34202 0.939693 0.5)
 84 arc 24 29 (0.17101 0.469846 0.5)
 85 arc 20 23 (0.939693 0.34202 0.5)
 86 arc 23 28 (0.34202 0.939693 0.5)
 87 arc 11 16 (-0.469846 0.17101 -0.5)
 88 arc 16 10 (-0.17101 0.469846 -0.5)
 89 arc 12 15 (-0.939693 0.34202 -0.5)
 90 arc 15 9 (-0.34202 0.939693 -0.5)
 91 arc 30 35 (-0.469846 0.17101 0.5)
 92 arc 35 29 (-0.17101 0.469846 0.5)
 93 arc 31 34 (-0.939693 0.34202 0.5)
 94 arc 34 28 (-0.34202 0.939693 0.5)
95 );
96
97 boundary
98 (
           down<br>{
\begin{array}{c} 100 \\ 101 \end{array}101 type symmetryPlane;<br>
102 faces
                f \overline{a}ces
\frac{103}{104}104 (0 1 20 19)
105 (1 2 21 20)
106 (12 11 30 31)
^{107}_{108} (13 12 31 32)
           \begin{matrix} \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{matrix}\frac{109}{110}right
111 \{112 type patch;<br>
113 faces
                f \overline{a} \overline{c} es
114 (
115 (2 3 22 21)
116 (3 6 25 22)
\begin{array}{ccc} 117 & & \\ 118 & & \end{array} ) ;
118<br>119
           up<br>{
\begin{array}{c} 120 \\ 121 \end{array}121 type symmetryPlane;<br>122 faces
                faces<br>(
\frac{123}{124}124 (7 8 27 26)
125 (6 7 26 25)
126 (8 18 37 27)
\begin{array}{cc} 127 & (18 \t17 \t36 \t37) \\ 128 & (18 \t17 \t36 \t37) \end{array}\rightarrow\frac{129}{130}\det\frac{131}{132}132 type patch;<br>
133 faces
                faces134 (
135 (14 13 32 33)
136 (17 14 33 36)
\begin{array}{ccc} \n 137 & & \rightarrow & \rightarrow & \n 138 & & \rightarrow & \n \end{array}138<br>139
           cylinder
140 {<br>141141 type symmetry;<br>
142 faces
                f \acute{a}ces
\frac{143}{144}144 (10 5 24 29)
145 (5 0 19 24)
146 (16 10 29 35)
147 (11 16 35 30)
\begin{array}{ccc} 148 & & \\ 149 & & \end{array} );
\begin{array}{c} 149 \\ 150 \end{array}150 );
151
152 mergePatchPairs<br>153 (
153 (
154 );
```
 // \* //

# 2.2.4 Boundary conditions and initial fields

Edit the case files to set the boundary conditions in accordance with the problem description in Figure [2.15,](#page-44-0) i.e. the left boundary should be an Inlet, the right boundary should be an Outlet and the down and cylinder boundaries should be symmetryPlane. The top boundary conditions is chosen so that we can make the most genuine comparison with our analytical solution which uses the assumption that the domain is infinite in the  $y$ direction. The result is that the normal gradient of U is small along a plane coinciding with our boundary. We therefore impose the condition that the normal component is zero, *i.e.* specify the boundary as a symmetryPlane, thereby ensuring that the comparison with the analytical is reasonable.

## 2.2.5 Running the case

No fluid properties need be specified in this problem since the flow is assumed to be incompressible and inviscid. In the system subdirectory, the controlDict specifies the control parameters for the run. Note that since we assume steady flow, we only run for 1 time step:

```
1 /*--------------------------------*- C++ -*----------------------------------*\
2 | ========= | |
3 | \\ / F ield | OpenFOAM: The Open Source CFD Toolbox
4 | \\ / 0 peration | Version: v2006<br>5 | \\ / A nd | Website: www.org
5 | \\ / A nd | Website: www.openfoam.com |
6 | \setminus\setminus M anipulation
7 \*---------------------------------------------------------------------------*/
\begin{array}{cc} 8 & \text{FoamFile} \\ 9 & 4 \end{array}9 {
10 version<br>11 format
10 version 2.0;<br>
11 format ascii;<br>
12 class dictio
12 class dictionary;<br>
13 location "system":
13 location<br>14 object
                    controlDict;
\begin{matrix} 15 & 7 \\ 16 & 7 \end{matrix}16 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
17
18 application potentialFoam;
19
20 startFrom latestTime;
21
22 startTime 0;
23
24 stopAt nextWrite;
25
26 endTime 1;
27
28 deltaT 1;
29
30 writeControl timeStep;
31
32 writeInterval 1;
33
34 purgeWrite 0;
35
36 writeFormat ascii;
37
38 writePrecision 6;
39
40 writeCompression off;
41
42 timeFormat general;
43
44 timePrecision 6;
45
46 runTimeModifiable true;
47
48 functions
49 {
50 error
```

```
51 {
52 name error;<br>53 type coded;
                         coded;
54 libs (utilityFunctionObjects);
55
56 codeEnd
\frac{57}{58} #{
                     // Lookup U
59 Info<< "Looking up field U\n" << endl;
60 const volVectorField& U = mesh().lookupObject<volVectorField>("U");
61
62 Info<< "Reading inlet velocity uInfX\n" << endl;
63
64 scalar ULeft = 0.0<br>65 label leftI = mesh
                     label leftI = mesh().boundaryMesh().findPatchID("left");
66 const fvPatchVectorField& fvp = U.boundaryField()[leftI];
67 if (fvp.size())
 68 {
69 ULeft = fvp[0].x();
 70 }
71 reduce(ULeft, maxOp<scalar>());
72
73 dimensionedScalar uInfX("uInfx", dimVelocity, ULeft);
74
75 Info<< "U at inlet = " << uInfX.value() << " m/s" << endl;
76
77
78 scalar magCylinder = 0.0;
79 label cyl\overline{1} = mesh().boundaryMesh().findPatchID("cylinder");
80 const fvPatchVectorField& cylFvp = mesh().C().boundaryField()[cylI];
81 if (cylFvp.size())
 82 \left\{ \begin{array}{ccc} 82 & \frac{1}{2} &82 \qquad \qquad f<br>
83 magCylinder = mag(cylFvp[0]);
 84 }
85 reduce(magCylinder, maxOp<scalar>());
86
87 dimensionedScalar radius("radius", dimLength, magCylinder);
88
89 Info<< "Cylinder radius = " << radius.value() << " m" << endl;
9091 volVectorField UA<br>92 (
 92 (
93 IOobject
 94 (
^{95} ^{95} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96} ^{96\begin{array}{c} \text{vol} \\ \text{sech}(\text{)}\text{.time}(\text{)}.time(\text{)}\text{.timeName}(\text{)}. \end{array}97 U.mesh(),
 98 IOobject::NO_READ,
99 IOobject::AUTO_WRITE
100 ),
101 U
\left.\begin{array}{ccc} 102 & \hspace{3.1cm} & \hspace{3.1cm} \end{array}\right);103
104 Info<< "\nEvaluating analytical solution" << endl;
105
106 const volVectorField& centres = UA.mesh().C();
107 volScalarField magCentres(mag(centres));
108 volScalarField theta(acos((centres & vector(1,0,0))/magCentres));
109
110 volVectorField cs2theta<br>111 (
111 (
112 cos(2*theta)*vector(1,0,0)<br>+ sin(2*theta)*vector(0.1.0)
113 + \sin(2*theta)*vector(0,1,0)<br>114 );
114 );
115
116 UA = uInfX*(dimensionedVector(vector(1,0,0))<br>117 - pow((radius/magCentres).2)*cs2theta):
                       - pow((radius/magCentres),2)*cs2theta);
118
119 // Force writing of UA (since time has not changed)
120 UA.write();
121
122 volScalarField error("error", mag(U-UA)/mag(UA));
123
124 Info<<"Writing relative error in U to " << error.objectPath() 125 << endl:
                          125 << endl;
126
127 error.write();
\begin{array}{@{}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{1em}}c@{\hspace{\frac{129}{130} }
130 }
131
132
133 // ************************************************************************* //
```
potentialFoam executes an iterative loop around the pressure equation which it solves in order that explicit terms relating to non-orthogonal correction in the Laplacian term may be updated in successive iterations. The number of iterations around the pressure equation is controlled by the nNonOrthogonalCorrectors keyword in the fvSolution dictionary. In the first instance we can set nNonOrthogonalCorrectors to 0 so that no loops are performed, *i.e.* the pressure equation is solved once, and there is no non-orthogonal correction. The solution is shown in Figure [2.17\(](#page-50-0)a) (at  $t = 1$ , when the steady-state simulation is complete). We expect the solution to show smooth streamlines passing across



<span id="page-50-0"></span>(c) Analytical solution

Figure 2.17: Streamlines of potential flow

the domain as in the analytical solution in Figure [2.17\(](#page-50-0)c), yet there is clearly some error in the regions where there is high non-orthogonality in the mesh,  $e.g.$  at the join of blocks 0, 1 and 3. The case can be run a second time with some non-orthogonal correction by setting nNonOrthogonalCorrectors to 3. The solution shows smooth streamlines with no significant error due to non-orthogonality as shown in Figure [2.17\(](#page-50-0)b).

# 2.3 Magnetohydrodynamic flow of a liquid

Tutorial path:

• \$FOAM\_[TUTORIALS/electromagnetics/mhdFoam/hartmann](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/electromagnetics/mhdFoam/hartmann)

In this example we shall investigate the flow of an electrically-conducting liquid through a magnetic field. The problem belongs to the branch of fluid dynamics known as magnetohydrodynamics (MHD), simulated using the mhdFoam solver.

# 2.3.1 Problem specification

This case is known as the Hartmann problem, chosen as it contains an analytical solution with which **mhdFoam** can be validated. It is defined as follows:

**Solution domain** The domain is 2 dimensional and consists of flow along two parallel plates as shown in Fig. [2.18.](#page-51-0)



<span id="page-51-0"></span>Figure 2.18: Geometry of the Hartmann problem

## Governing equations

• Mass continuity for incompressible fluid

$$
\nabla \cdot \mathbf{U} = 0 \tag{2.16}
$$

• Momentum equation for incompressible fluid

$$
\frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot (\mathbf{U} \mathbf{U}) + \nabla \cdot (2 \mathbf{B} \Gamma_{\mathbf{B} \mathbf{U}} \mathbf{B}) + \nabla \cdot (\nu \mathbf{U}) + \nabla (\Gamma_{\mathbf{B} \mathbf{U}} \mathbf{B} \cdot \mathbf{B}) = -\nabla p \tag{2.17}
$$

where **B** is the magnetic flux density,  $\Gamma_{BU} = (2\mu\rho)^{-1}$ .

• Maxwell's equations

<span id="page-51-1"></span>
$$
\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}
$$
 (2.18)

where **E** is the electric field strength.

$$
\nabla \cdot \mathbf{B} = 0 \tag{2.19}
$$

<span id="page-51-2"></span>
$$
\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} = \mathbf{J}
$$
 (2.20)

assuming  $\partial \mathbf{D}/\partial t \ll \mathbf{J}$ . Here, **H** is the magnetic field strength, **J** is the current density and D is the electric flux density.

• Charge continuity

$$
\nabla \cdot \mathbf{J} = 0 \tag{2.21}
$$

• Constitutive law

<span id="page-52-0"></span>
$$
\mathbf{B} = \mu \mathbf{H} \tag{2.22}
$$

• Ohm's law

$$
\mathbf{J} = \sigma \left( \mathbf{E} + \mathbf{U} \times \mathbf{B} \right) \tag{2.23}
$$

• Combining Equation [2.18,](#page-51-1) Equation [2.20,](#page-51-2) Equation [2.23,](#page-52-0) and taking the curl

$$
\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{U} \mathbf{B}) - \nabla \cdot (\phi_{\mathbf{B}} \mathbf{U}) - \nabla \cdot (\Gamma_{\mathbf{B}} \mathbf{B}) = 0 \tag{2.24}
$$

#### Boundary conditions

- inlet is specified the inlet condition with fixed velocity  $\mathbf{U} = (1, 0, 0)$  m/s;
- outlet is specified as the outlet with with fixed pressure  $p = 0$  Pa;
- upperWall is specified as a wall where  $B = (0, 20, 0)$  T.
- lowerWall is specified as a wall where  $B = (0, 20, 0)$  T.
- front and back boundaries are specified as empty.

**Initial conditions**  $U = 0$  m/s,  $p = 100$  Pa,  $B = (0, 20, 0)$  T.

#### Transport properties

- Kinematic viscosity  $\nu = 1$  Pas
- Density  $\rho = 1 \text{ kg m/s}$
- Electrical conductivity  $\sigma = 1$  ( $\Omega$  m)<sup>-1</sup>
- Permeability  $\mu = 1$  H/m

Solver name mhdFoam: an incompressible laminar magneto-hydrodynamics code.

Case name hartmann case located in the \$FOAM\_TUTORIALS/electromagnetics/mhd-Foam directory.

#### 2.3.2 Mesh generation

The geometry is simply modelled with 100 cells in the x-direction and 40 cells in the y-direction; the set of vertices and blocks are given in the mesh description file below:

<sup>1</sup> /\*--------------------------------\*- C++ -\*----------------------------------\*\ <sup>2</sup> | ========= | | 3 | \\ / F ield | OpenFOAM: The Open Source CFD Toolbox | <sup>4</sup> | \\ / O peration | Version: v2006 | 5 | \\ / A nd | Website: www.openfoam.com  $6$  |  $\setminus\setminus$  M anipulation | <sup>7</sup> \\*---\*/ <sup>8</sup> FoamFile  $\begin{array}{c} 9 \\ 10 \end{array}$ 10 version 2.0;<br>
11 format ascii;  $\begin{array}{cc}\n 11 & \text{format} \\
 12 & \text{class}\n \end{array}$ 12 class dictionary; 13 object blockMeshDict; <sup>14</sup> }

```
15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 1;
18
\frac{19}{20} vertices
\frac{20}{21}21 (0 -1 0)22 (20 -1 0)23 (20 1 0)
24 (0 1 0)
25 (0 -1 0.1)26 (20 -1 0.1)27 (20 1 0.1)
28 (0 1 0.1)
\frac{20}{29} );
30
31 blocks
32 (
33 hex (0 1 2 3 4 5 6 7) (100 40 1) simpleGrading (1 1 1)
34 );
35
36 edges
37 (
38 );
39
40 boundary
\frac{41}{42} (
             inlet<br>{
\frac{43}{44}44 type patch;<br>45 faces
                   \det faces
\frac{46}{47}\frac{47}{48} (0 4 7 3)
             \rightarrow );
\frac{49}{50}outlet<br>{
\begin{array}{c} 51 \\ 52 \end{array}52 type patch;<br>53 faces
                   faces<sup>3</sup>
\begin{array}{c} 54 \\ 55 \end{array}\frac{55}{55} (2 6 5 1)<br>
\frac{5}{56} );
                   );
\frac{57}{58}lowerWall
59 6060 type patch;<br>61 faces
\begin{array}{ccc}\n61 & & \text{faces} \\
62 & & \text{(} & \text{()}\n\end{array}62 (
\begin{array}{c} 63 \\ 63 \\ 64 \end{array} (1 5 4 0)
             \rightarrow );
65 }
             upperWall
\frac{67}{68}68 type patch;
69 faces
70 (
\begin{array}{cc} \begin{array}{cc} 71 \\ 72 \end{array} \\ \begin{array}{cc} \end{array} \\ \begin{array}{cc} \end{array} \\ \end{array}
(3 7 6 2)
                    );
\frac{73}{74}74 frontAndBack<br>75 {
\begin{matrix} 75 & \phantom{0} \phantom{0} 1 \\ 76 & \phantom{0} \end{matrix}76 type empty;<br>77 faces
\begin{array}{ccc}\n\frac{77}{78} & \text{faces} \\
\frac{78}{78} & \text{Gauss}\n\end{array}78 (
\begin{array}{cc}\n 79 \\
 80 \\
 \end{array}
(0 3 2 1)<br>
(4 5 6 7)
\begin{array}{cc} 80 & 4567 \ 81 & 31 \end{array}81 );
\frac{82}{83}) ;
84
85 mergePatchPairs
86 (
87 );
88
89 // ************************************************************************* //
```
# 2.3.3 Running the case

The user can run the case and view results in ParaView. It is also useful at this stage to run the Ucomponents utility to convert the U vector field into individual scalar components. MHD flow is governed by, amongst other things, the Hartmann number which is a measure of the ratio of electromagnetic body force to viscous force

$$
M = BL\sqrt{\frac{\sigma}{\rho\nu}}\tag{2.25}
$$

where L is the characteristic length scale. In this case with  $B_y = 20$  T,  $M = 20$  and the electromagnetic body forces dominate the viscous forces. Consequently with the flow fairly steady at  $t = 2$  s the velocity profile is almost planar, viewed at a cross section midway along the domain  $x = 10$  m. The user can plot a graph of the profile of  $U_x$  in dxFoam. Now the user should reduce the magnetic flux density B to 1 Tand re-run the



<span id="page-54-0"></span>Figure 2.19: Velocity profile in the Hartmann problem for  $B_y = 1$  T and  $B_y = 20$  T.

code and Ucomponents. In this case,  $M = 1$  and the electromagnetic body forces no longer dominate. The velocity profile consequently takes on the parabolic form, characteristic of Poiseuille flow as shown in Figure [2.19.](#page-54-0) To validate the code the analytical solution for the velocity profile  $U_x$  is superimposed in Figure [2.19,](#page-54-0) given by:

$$
\frac{U_x(y)}{U_x(0)} = \frac{\cosh M - \cosh M(y/L)}{\cosh M - 1}
$$
\n
$$
(2.26)
$$

where the characteristic length  $L$  is half the width of the domain, *i.e.* 1 m.

# Chapter 3

# Compressible flow

# 3.1 Steady turbulent flow over a backward-facing step

Tutorial path:

• \$FOAM [TUTORIALS/incompressible/simpleFoam/pitzDaily](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/incompressible/simpleFoam/pitzDaily)

In this example we shall investigate steady turbulent flow over a backward-facing step. The problem description is taken from one used by Pitz and Daily in an experimental investigation [\*\*] against which the computed solution can be compared. This example introduces the following OpenFOAM features for the first time:

- generation of a mesh using blockMesh using full mesh grading capability;
- steady turbulent flow.

# 3.1.1 Problem specification

The problem is defined as follows:

Solution domain The domain is 2 dimensional, consisting of a short inlet, a backwardfacing step and converging nozzle at outlet as shown in Figure [3.1.](#page-57-0)



<span id="page-57-0"></span>Figure 3.1: Geometry of backward-facing step

#### Governing equations

• Mass continuity for incompressible flow

$$
\nabla \cdot \mathbf{U} = 0 \tag{3.1}
$$

• Steady flow momentum equation

$$
\nabla \bullet (\mathbf{U}\mathbf{U}) + \nabla \bullet \mathbf{R} = -\nabla p \tag{3.2}
$$

where p is kinematic pressure and (in slightly over-simplistic terms)  $\mathbf{R} =$  $\nu_{eff} \nabla U$  is the viscous stress term with an effective kinematic viscosity  $\nu_{eff}$ , calculated from selected transport and turbulence models.

**Initial conditions**  $U = 0$  m/s,  $p = 0$  Pa — required in OpenFOAM input files but not necessary for the solution since the problem is steady-state.

#### Boundary conditions

- Inlet (left) with fixed velocity  $\mathbf{U} = (10, 0, 0)$  m/s;
- Outlet (right) with fixed pressure  $p = 0$  Pa;
- No-slip walls on other boundaries.

#### Transport properties

• Kinematic viscosity of air  $\nu = \mu/\rho = 18.1 \times 10^{-6}/1.293 = 14.0 \text{ }\mu\text{m}^2/\text{s}$ 

#### Turbulence model

- Standard  $k \epsilon$ ;
- Coefficients:  $C_{\mu} = 0.09; C_1 = 1.44; C_2 = 1.92; \alpha_k = 1; \alpha_{\epsilon} = 0.76923.$

**Solver name simpleFoam:** an implementation for steady incompressible flow.

Case name pitzDaily, located in the \$FOAM TUTORIALS/incompressible/simpleFoam directory.

The problem is solved using simpleFoam, so-called as it is an implementation for steady flow using the SIMPLE algorithm. The solver has full access to all the turbulence models in the incompressibleTurbulenceModels library and the non-Newtonian models incompressibleTransportModels library of the standard OpenFOAM release.

# 3.1.2 Mesh generation

We expect that the flow in this problem is reasonably complex and an optimum solution will require grading of the mesh. In general, the regions of highest shear are particularly critical, requiring a finer mesh than in the regions of low shear. We can anticipate where high shear will occur by considering what the solution might be in advance of any calculation. At the inlet we have strong uniform flow in the  $x$  direction and, as it passes over the step, it generates shear on the fluid below, generating a vortex in the bottom half of the domain. The regions of high shear will therefore be close to the centreline of the domain and close to the walls.

The domain is subdivided into 12 blocks as shown in Figure [3.2.](#page-58-0)



<span id="page-58-0"></span>Figure 3.2: Blocks in backward-facing step

The mesh is 3 dimensional, as always in OpenFOAM, so in Figure [3.2](#page-58-0) we are viewing the back plane along  $z = -0.5$ . The full set of vertices and blocks are given in the mesh description file below:

```
1 /*--------------------------------*- C++ -*----------------------------------*\
 2 | ========= | |
 3 | \\   / F ield     | OpenFOAM: The Open Source CFD Toolbox     |
4 | \\ / O peration | Version: v2006 |
 5 | \\ / And | Website: www.openfoam.com<br>6 | \\/ Manipulation |
6 | \setminus\setminus M anipulation |
 7 \*---------------------------------------------------------------------------*/
8 FoamFile
\begin{array}{cc} 9 & \text{f} \\ 10 & \text{f} \end{array}10 version 2.0;<br>
11 format ascii;
          format<br>class
12 class dictionary<br>
13 object blockMeshD
                        blockMeshDict;
\begin{array}{c} 14 \\ 15 \end{array}15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 0.001;
18
\frac{19}{20} vertices
2021 \quad (-20.6 \ 0 \ -0.5)22 \left( -20.6 \right. 25.4 \left. -0.5 \right)23 (0 -25.4 -0.5)24 \hspace{1.5cm} (0 \hspace{.1cm} 0 \hspace{.1cm} -0.5)25 (0, 25.4, -0.5)26 (206 - 25.4 - 0.5)27 (206 0 -0.5)
28 (206 25.4 -0.5)
29 (290 -16.6 -0.5)30 \quad (290 \quad 0 \quad -0.5)\frac{30}{31} (290 16.6 -0.5)
32
33 \left( -20.6 \ 0 \ 0.5 \right)34 (-20.6 25.4 0.5)
35 \left(0 - 25.4 \right. 0.5)36 (0 0 0.5)
37 (0 25.4 0.5)
38 (206 -25.4 0.5)39 (206 0 0.5)
40 (206 25.4 0.5)
41 \hspace{1.5cm} (290 -16.6 \ 0.5)42 (290 0 0.5)
43 (290 16.6 0.5)
\begin{matrix} 43 \\ 44 \end{matrix} );
45
46 negY
\frac{47}{48} (
\begin{array}{ccc} 48 & (2 \ 4 \ 1) \\ 49 & (1 \ 3 \ 0) \end{array}\begin{array}{cc} 49 \\ 50 \end{array} (1 3 0.3)
     );
51
52 posY
\begin{array}{c} 53 \\ 54 \end{array} (
54 (1 4 2)
55 (2 3 4)
56 (2 4 0.25)
57 );
58
59 posYR
\begin{matrix}60 & 61\end{matrix}\begin{array}{cc} 61 & (2 \ 1 \ 1) \\ 62 & (1 \ 1 \ 0) \end{array}\begin{array}{c} 0.62 \ 62 \ 63 \end{array} (1 1 0.25)
     ):
64
65
66 blocks
rac{67}{68}68 hex (0 3 4 1 11 14 15 12)
69 (18 30 1)
70 simpleGrading (0.5 $posY 1)
71
72 hex (2 5 6 3 13 16 17 14)
73 (180 27 1)
^{74} edgeGrading (4 4 4 4 $negY 1 1 $negY 1 1 1 1)
75
76 hex (3 6 7 4 14 17 18 15)
77 (180 30 1)
78 edgeGrading (4 4 4 4 $posY $posYR $posYR $posY 1 1 1 1)
79
80 hex (5 8 9 6 16 19 20 17)
81 (25 27 1)
82 simpleGrading (2.5 1 1)
83
84 hex (6 9 10 7 17 20 21 18)
85 (25 30 1)
```

```
86 simpleGrading (2.5 $posYR 1)
 87 );
 88
 89 edges
 90 (
 91 );
 92
 93 boundary
 \frac{94}{95} (
             inlet
 96 {
 97 type patch;
 98 faces
 99 (
100 (0 1 12 11)
\begin{array}{ccc} \n\frac{101}{102} & & \rightarrow \n\end{array}\frac{102}{103}outlet
104 {
105 type patch;
106 faces
107 (
108 (8 9 20 19)<br>
109 (9 10 21 20
                            10, 21, 20)\begin{matrix} 110 \\ 111 \end{matrix}  );
\begin{array}{c} 111 \\ 112 \end{array}upperWall
\begin{array}{c} 113 \\ 114 \end{array}114 type wall;<br>115 faces
                  f \overline{\text{aces}}116<br>117
117 (1 4 15 12)
118 (4 7 18 15)
118 \overline{4} \overline{7} \overline{18} \overline{15}<br>
119 (7 \overline{10} \overline{21} \overline{18})<br>
120 ):
\begin{array}{ccc} 120 & & \\ 121 & & \end{array} );
121 }
122 lowerWall
123 {
124 type wall;<br>125 faces
125 faces
126 (
127 (0 3 14 11)
128 (3 2 13 14)
129 (2 5 16 13)
130 (5 8 19 16)
\frac{131}{131} );
132 }
133 frontAndBack
134<br>135
                  type empty;
136 faces
137 (
\begin{array}{cccc} \n & 138 \\
139 \\
140 \\
141 \\
142\n\end{array} & (0 3 4 1) \\
 & (2 5 6 3) \\
 & (3 6 7 4) \\
 & (5 8 9 6) \\
 & (6 9 10 7) \\
 & (7 12 12) \\
 & (10 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 11) \\
 & (11 10 1139 (2 5 6 3)
140 (3 6 7 4)
141 (5 8 9 6)
142 (6 9 10 7)
143 (11 14 15 12)
144 (13 16 17 14)
143
(11 14 15 12)<br>
144
(13 16 17 14)<br>
145
(14 17 18 15)<br>
146
(16 19 20 17)
146 (16 19 20 17)
147 (17 20 21 18)
\begin{array}{c} 148 \\ 149 \end{array} );
149<br>150
       ):
151
152 // ************************************************************************* //
```
A major feature of this problem is the use of the full mesh grading capability of blockMesh that is described in section 4.3.1 of the User Guide. The user can see that blocks 4,5 and 6 use the full list of 12 expansion ratios. The expansion ratios correspond to each edge of the block, the first 4 to the edges aligned in the local  $x_1$  direction, the second 4 to the edges in the local  $x_2$  direction and the last 4 to the edges in the local  $x_3$ direction. In blocks 4, 5, and 6, the ratios are equal for all edges in the local  $x_1$  and  $x_3$ directions but not for the edges in the  $x_2$  direction that corresponds in all blocks to the global y. If we consider the ratios used in relation to the block definition in section 4.3.1 of the User Guide, we realize that different gradings have been prescribed along the left and right edges in blocks 4,5 and 6 in Figure [3.2.](#page-58-0) The purpose of this differential grading is to generate a fine mesh close to the most critical region of flow, the corner of the step, and allow it to expand into the rest of the domain.

The mesh can be generated using blockMesh from the command line and viewed as described in previous examples.

# 3.1.3 Boundary conditions and initial fields

Edit the case files to set the initial and boundary fields for velocity  $U$ , pressure p, turbulent kinetic energy k and dissipation rate  $\varepsilon$ . The boundary conditions can be specified as: the upper and lower walls are set to Wall, the left patch to Inlet and the right patch to Outlet. These physical boundary conditions require us to specify a fixedValue at the inlet on U, k and  $\varepsilon$ . U is given in the problem specification, but the values of k and  $\epsilon$  must be chosen by the user in a similar manner to that described in section [2.1.8.1](#page-36-0) of the User Guide. We assume that the inlet turbulence is isotropic and estimate the fluctuations to be 5% of U at the inlet. We have

$$
U_x' = U_y' = U_z' = \frac{5}{100} 10 = 0.5 \text{ m/s}
$$
\n(3.3)

and

$$
k = \frac{3}{2}(0.5)^2 = 0.375 \text{ m}^2/\text{s}^2
$$
\n(3.4)

If we estimate the turbulent length scale  $l$  to be 10% of the width of the inlet then

$$
\varepsilon = \frac{C_{\mu}^{0.75} k^{1.5}}{l} = \frac{0.09^{0.75} 0.375^{1.5}}{0.1 \times 25.4 \times 10^{-3}} = 14.855 \,\mathrm{m}^2/\mathrm{s}^3 \tag{3.5}
$$

At the outlet we need only specify the pressure  $p = 0Pa$ .

## 3.1.4 Case control

The choices of *fvSchemes* are as follows: the timeScheme should be steadyState; the gradSchemes and laplacianSchemes should be set as default to Gauss; and, the divSchemes should be set to upwind to ensure boundedness.

Special attention should be paid to the solver settings of the  $\mathit{fvSolution}$  dictionary. Although the top level simpleFoam code contains only equations for p and U, the turbulence model solves equations for  $k, \varepsilon$  and  $\mathbf{R}$ , and tolerance settings are required for all 5 equations. A tolerance of  $10^{-5}$  and relTol of 0.1 are acceptable for all variables with the exception of p when  $10^{-6}$  and 0.01 are recommended. Under-relaxation of the solution is required since the problem is steady. A relaxationFactor of 0.7 is acceptable for U, k, and  $\varepsilon$  but 0.3 is required for p to avoid numerical instability.

Finally, in the *controlDict* dictionary, the time step deltar should be set to 1 since in steady state cases such as this is effectively an iteration counter. With benefit of hindsight we know that the solution requires 1000 iterations reach reasonable convergence, hence endTime is set to 1000. Ensure that the writeInterval is sufficiently high,  $e.g.$  50, that you will not fill the hard disk with data during run time.

# 3.1.5 Running the case and post-processing

Run the case and post-process the results. After a few iterations, e.g. 50, a vortex develops beneath the corner of the step that is the height of the step but narrow in the x-direction as shown by the vector plot of velocities is shown Figure  $3.3(a)$  $3.3(a)$ . Over several iterations



<span id="page-62-0"></span>(c) Streamlines at 1000 iterations

Figure 3.3: Development of a vortex in the backward-facing step.

the vortex stretches in the x-direction from the step to the outlet until at  $1000$  iterations the system reaches a steady-state in which the vortex is fully developed as shown in Figure  $3.3(b-c)$  $3.3(b-c)$ .

# 3.2 Supersonic flow over a forward-facing step

Tutorial path:

• \$FOAM\_[TUTORIALS/compressible/sonicFoam/laminar/forwardStep](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/compressible/sonicFoam/laminar/forwardStep)

In this example we shall investigate supersonic flow over a forward-facing step. The problem description involves a flow of Mach 3 at an inlet to a rectangular geometry with a step near the inlet region that generates shock waves.

This example introduces the following OpenFOAM features for the first time:

• supersonic flow:

# 3.2.1 Problem specification

The problem is defined as follows:

Solution domain The domain is 2 dimensional and consists of a short inlet section followed by a forward-facing step of 20% the height of the section as shown in Figure [3.4](#page-63-0)



<span id="page-63-0"></span>Figure 3.4: Geometry of the forward step geometry

#### Governing equations

• Mass continuity

$$
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0 \tag{3.6}
$$

• Ideal gas

$$
p = \rho RT \tag{3.7}
$$

• Momentum equation for Newtonian fluid

$$
\frac{\partial \rho \mathbf{U}}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) - \nabla \cdot \mu \nabla \mathbf{U} = -\nabla p \tag{3.8}
$$

• Energy equation for fluid (ignoring some viscous terms),  $e = C_vT$ , with Fourier's Law  $\mathbf{q} = -k\nabla T$ 

$$
\frac{\partial \rho e}{\partial t} + \nabla \cdot (\rho \mathbf{U} e) - \nabla \cdot \left(\frac{k}{C_v}\right) \nabla e = p \nabla \cdot \mathbf{U}
$$
\n(3.9)

*Initial conditions*  $U = 0$  m/s,  $p = 1$  Pa,  $T = 1$  K.

#### Boundary conditions

- Inlet (left) with fixedValue for velocity  $U = 3$  m/s = Mach 3, pressure  $p = 1$  Pa and temperature  $T = 1$  K;
- Outlet (right) with zeroGradient on  $U$ ,  $p$  and  $T$ ;
- No-slip adiabatic wall (bottom);
- Symmetry plane (top).

#### Transport properties

• Dynamic viscosity of air  $\mu = 18.1 \mu \text{Pa s}$ 

#### Thermodynamic properties

- Specific heat at constant volume  $C_v = 1.78571 \text{ J/kg K}$
- Gas constant  $R = 0.714286 \text{ J/kg K}$
- Conductivity  $k = 32.3 \text{ \mu W/m K}$

Case name forwardStep case located in the \$FOAM\_TUTORIALS/compressible/sonic-Foam/laminar directory.

**Solver name sonicFoam:** an implementation for compressible trans-sonic/supersonic laminar gas flow.

The case is designed such that the speed of sound of the gas  $c = \sqrt{\gamma RT} = 1$  m/s, the consequence being that the velocities are directly equivalent to the Mach number, e.g. the inlet velocity of 3 m/s is equivalent to Mach 3. This speed of sound calculation can be verified using the relationship for a perfect gas,  $C_p - Cv = R$ , *i.e.* the ratio of specific heats

$$
\gamma = C_p/C_v = \frac{R}{C_v} + 1\tag{3.10}
$$

# 3.2.2 Mesh generation

The mesh used in this case is relatively simple, specified with uniform rectangular cells of length 0.06 m in the x direction and 0.05 m in the y direction. The geometry can simply be divided into 3 blocks, one below the top of the step, and two above the step, one either side of the step front. The full set of vertices and blocks are given in the mesh description file below:

```
1 /*--------------------------------*- C++ -*----------------------------------*\
 2 | ========= | |
 3 | \\   / F ield     | OpenFOAM: The Open Source CFD Toolbox     |
4 | \\ / O peration | Version: v2006 |
5 | \\ / And | Website: www.openfoam.com
6 | \setminus\setminus M anipulation |
 7 \*---------------------------------------------------------------------------*/
8 FoamFile
\begin{matrix}9\\10\end{matrix}\begin{array}{ccc} 10 & \text{version} & 2.0; \\ 11 & \text{format} & \text{ascii}: \end{array}11 format<br>12 class
12 class dictionary<br>
13 object blockMeshD
                     blockMeshDict;
\frac{14}{15}15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 1;
```

```
18
\begin{array}{cc} 19 & \text{vertices} \\ 20 & \text{ } \end{array}\frac{20}{21}21 (0 0 -0.05)
 22 \hspace{1.5cm} (0.6 \hspace{1.2cm} 0 \hspace{1.2cm} -0.05)23 (0\ 0.2\ -0.05)24 \hspace{1.5cm} (0.6 \hspace{1.2cm} 0.2 \hspace{1.2cm} -0.05)25 (3 \t0.2 \t-0.05)26 (0 \t1 \t-0.05)27 (0.6 1 -0.05)
 28 (3 \t1 \t-0.05)29 (0 0 0.05)
 30 (0.6 0 0.05)
 31 (0 0.2 0.05)
 32 \hspace{1.5cm} (0.6 \hspace{1.5cm} 0.2 \hspace{1.5cm} 0.05)33 (3 0.2 0.05)
 34 (0 1 0.05)
 35 (0.6 1 0.05)
 36 (3 1 0.05)
37 );
38
39 blocks
\begin{array}{cc} 40 & 6 \\ 41 & 6 \end{array}hex (0 1 3 2 8 9 11 10) (25 10 1) simpleGrading (1 1 1)
42 hex (2 3 6 5 10 11 14 13) (25 40 1) simpleGrading (1 1 1)
43 hex (3 4 7 6 11 12 15 14) (100 40 1) simpleGrading (1 1 1)
44 );
45
46 edges
\frac{47}{48}\int ;
49
50 boundary
\frac{51}{52} (
             inlet<br>{
\begin{array}{c} 53 \\ 54 \end{array}54 type patch;<br>55 faces
55 faces<sup>55</sup>
 56 (
\begin{array}{cc} 57 \\ 58 \end{array} (0 8 10 2)<br>58 (2 10 13 5
\begin{array}{c} 58 \\ 58 \\ 59 \end{array} (2 10 13 5)
             \rightarrow\begin{array}{c} 60 \\ 61 \end{array}outlet<br>{
\begin{array}{c} 62 \\ 63 \end{array}63 type patch;<br>64 faces
                   f \overline{a} \overline{c} es
\begin{array}{c} 65 \\ 66 \end{array}\begin{array}{cc} 66 & 4 \end{array} (4 7 15 12)
             \lambda );
68 }
             bottom<br>{
\begin{array}{c} 70 \\ 71 \end{array}71 type symmetryPlane;<br>
72 faces
                   faces
\frac{73}{74}\frac{74}{75} (0 1 9 8)
             \rightarrow\frac{76}{77}top<br>{
78 {
                   type symmetryPlane;
\begin{array}{ccc}\n 80 & \text{faces} \\
 81 & \text{G} \\
 \end{array}81 (
 82 (5 13 14 6)
 83 (6 14 15 7)
\begin{array}{ccc} 84 & & \\ 85 & & \\ 85 & & \end{array} );
             }
 86 obstacle
 87 {
88 type patch;<br>89 faces
                   \det faces
90 (
 91 (1 3 11 9)
 92 (3 4 12 11)
\begin{array}{ccc} 92 \\ 93 \\ 94 \end{array} ) ;
94 }
       );
96
97 mergePatchPairs
 98 (
 99 );
100
101 // ************************************************************************* //
```
# 3.2.3 Running the case

The case approaches a steady-state at some time after 10 s. The results for pressure at 2 s are shown in Figure [3.5.](#page-66-0) The results clearly show discontinuities in pressure, i.e. shock waves, emanating from ahead of the base of the step.



<span id="page-66-0"></span>Figure 3.5: Shock fronts in the forward step problem

## 3.2.4 Exercise

The user can examine the effect on the solution of increasing the inlet velocity.

# 3.3 Decompression of a tank internally pressurised with water

Tutorial path:

• \$FOAM\_[TUTORIALS/compressible/sonicLiquidFoam/decompressionTank](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/compressible/sonicLiquidFoam/decompressionTank)

In this example we shall investigate a problem of rapid opening of a pipe valve close to a pressurised liquid-filled tank. The prominent feature of the result in such cases is the propagation of pressure waves which must therefore be modelled as a compressible liquid.

This tutorial introduces the following OpenFOAM features for the first time:

- Mesh refinement
- Pressure waves in liquids

# 3.3.1 Problem specification

**Solution domain** The domain is 2 dimensional and consists of a tank with a small outflow pipe as shown in Figure [3.6](#page-67-0)



<span id="page-67-0"></span>Figure 3.6: Geometry of a tank with outflow pipe

Governing equations This problem requires a model for compressibility  $\psi$  in the fluid in order to be able to resolve waves propagating at a finite speed. A barotropic relationship is used to relate density  $\rho$  and pressure p are related to  $\psi$ .

• Mass continuity

$$
\frac{\partial \rho}{\partial t} + \nabla \bullet (\rho \mathbf{U}) = 0 \tag{3.11}
$$

• The barotropic relationship

<span id="page-67-1"></span>
$$
\frac{\partial \rho}{\partial p} = \frac{\rho}{K} = \psi \tag{3.12}
$$

where  $K$  is the bulk modulus

• Equation [3.12](#page-67-1) is linearised as

 $\rho \approx \rho_0 + \psi (p - p_0)$  (3.13)

where  $\rho_0$  and  $p_0$  are the reference density and pressure respectively such that  $\rho(p_0) = \rho_0.$ 

• Momentum equation for Newtonian fluid

$$
\frac{\partial \rho \mathbf{U}}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) - \nabla \cdot \mu \nabla \mathbf{U} = -\nabla p \tag{3.14}
$$

#### Boundary conditions

- outerWall is specified the wall condition;
- axis is specified as the symmetryPlane;
- nozzle is specified as a pressureOutlet where  $p = 0$  bar.
- front and back boundaries are specified as empty.

**Initial conditions**  $U = 0$  m/s,  $p = 100$  bar.

#### Transport properties

• Dynamic viscosity of water  $\mu = 1.0$  mPa s

#### Thermodynamic properties

- Density of water  $\rho = 1000 \text{ kg/m}^3$
- Reference pressure  $p_0 = 1$  bar
- Compressibility of water  $\psi = 4.54 \times 10^{-7} \text{ s}^2/\text{m}^2$

**Solver name sonicLiquidFoam**: a solver for compressible sonic laminar liquid flow.

Case name decompressionTank case located in the \$FOAM TUTORIALS/compressible/ sonicLiquidFoam directory.

## 3.3.2 Mesh Generation

The full geometry is modelled in this case; the set of vertices and blocks are given in the mesh description file below:

```
1 /*--------------------------------*- C++ -*----------------------------------*\
 2 | ========= | |
 3 | \\ / F ield | OpenFOAM: The Open Source CFD Toolbox |
4 | \\ / 0 peration | Version: v2006<br>5 | \\ / A nd | Website: www.org
 5 | \setminus\setminus / A nd | Website: www.openfoam.com 6 | \setminus\setminus / M anipulation |
6 | \\/ M anipulation | |
7 \*---------------------------------------------------------------------------*/
8 FoamFile
\frac{9}{10}10 version 2.0;<br>
11 format ascii;
11 format<br>12 class
12 class dictionary;
13 object blockMeshDict;
\frac{14}{15}15 // * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * //
16
17 scale 0.1;
18
19 vertices
\frac{20}{21}21 (0 \ 0 \ -0.1)22 \qquad (1 \ 0 \ -0.1)23 \hspace{1.5cm} (0 \hspace{0.1cm} 0.5 \hspace{0.1cm} -0.1)24 \left(1 \ 0.5 \ -0.1\right)25 (1.5 \t0.5 \t-0.1)26 (0\ 0.6\ -0.1)27 (1 \t0.6 \t-0.1)28 (1.5 \t0.6 \t-0.1)29 (0 \t3 \t-0.1)30 \left(1 \quad 3 \quad -0.1\right)\overline{31} \overline{0} \ \overline{0} \ \overline{0} \ \overline{0} \ \overline{1}
```

```
32 (1 0 0.1)
 33 (0 0.5 0.1)
 34 (1 0.5 0.1)
 35 (1.5 0.5 0.1)
 36 (0 0.6 0.1)
 37 (1 0.6 0.1)
 38 (1.5 0.6 0.1)
 39 (0 3 0.1)
 40 (1 3 0.1)
\frac{41}{41} );
42
43 blocks
44 (
45 hex (0 1 3 2 10 11 13 12) (30 20 1) simpleGrading (1 1 1)
 46 hex (2 3 6 5 12 13 16 15) (30 5 1) simpleGrading (1 1 1)
 47 hex (3 4 7 6 13 14 17 16) (25 5 1) simpleGrading (1 1 1)
48 hex (5 6 9 8 15 16 19 18) (30 95 1) simpleGrading (1 1 1)
49 );
50
51 edges
 52 (
 53 );
54
55 boundary
\begin{array}{c} 56 \\ 57 \end{array} (
          outerWall
58 {
59 type wall;<br>60 faces
\begin{array}{ccc}\n60 & & \text{faces} \\
61 & & \text{G} \\
\end{array}61 (
 62 (0 1 11 10)
 63 (1 3 13 11)
 (3 \t4 \t14 \t13)65 (7 6 16 17)
 66 (6 9 19 16)
 67 (9 8 18 19)
\begin{array}{ccc} 67 & & & \\ 68 & & & \\ 69 & & & \end{array}69 }
 70 axis
 71 {
<sup>71</sup> {<br><sup>72</sup> type symmetryPlane;<br><sup>73</sup> faces
              f \acute{a}ces
74\phantom{1}7575 (0 10 12 2)
 76 (2 12 15 5)
 77 (5 15 18 8)
\frac{78}{79} );
\frac{79}{80}\begin{array}{ccc}\n 80 & & \text{nozzle} \\
 81 & & \{ \end{array}81 \atop 82 {
82 type patch;<br>83 faces
\begin{array}{ccc}\n 83 & \text{faces} \\
 84 & \text{G} \\
 \end{array}84 (
85 (4 7 17 14)
              );
87 }
88 back<br>89 f
\begin{array}{c} 89 \\ 90 \end{array} \begin{array}{c} 5 \ 6 \end{array}90 type empty;
 91 faces
 92 (
 93 (0 2 3 1)
 94 (2 5 6 3)
 95 (3\ 6\ 7\ 4)96 (5 8 9 6)
\frac{97}{98} );
98 }
          \frac{1}{3} front
\frac{100}{101}101 type empty;<br>
102 faces
               \det faces
103<br>104104 (10 11 13 12)<br>105 (12 13 16 15)
105 (12 13 16 15)
106 (13 14 17 16)
106 (13 14 17 16)<br>
107 (15 16 19 18)<br>
108 );
          \rightarrow );
\frac{109}{110});
111
112 mergePatchPairs
113 (
114 );
115
116 // ************************************************************************* //
```
In order to improve the numerical accuracy, we shall use the reference level of 1 bar for the pressure field. Note that both the internal field level and the boundary conditions are offset by the reference level.

#### 3.3.3 Preparing the Run

Before we commence the setup of the calculation, we need to consider the characteristic velocity of the phenomenon we are trying to capture. In the case under consideration, the fluid velocity will be very small, but the pressure wave will propagate with the speed of sound in water. The speed of sound is calculated as:

$$
c = \sqrt{\frac{1}{\psi}} = \sqrt{\frac{1}{4.54 \times 10^{-7}}} = 1483.2 \text{m/s}.
$$
\n(3.15)

For the mesh described above, the characteristic mesh size is approximately 2 mm (note the scaling factor of 0.1 in the blockMeshDict file). Using

$$
Co = \frac{U \Delta t}{\Delta x} \tag{3.16}
$$

a reasonable time step is around  $\Delta t = 5 \times 10^{-7}$ s, giving the Co number of 0.35, based on the speed of sound. Also, note that the reported  $Co$  number by the code (associated with the convective velocity) will be two orders of magnitude smaller. As we are interested in the pressure wave propagation, we shall set the simulation time to 0.25 ms. For reference, the controlDict file is quoted below.



```
45
46 runTimeModifiable true;
47
48
49 // ************************************************************************* //
```
# 3.3.4 Running the case



<span id="page-71-0"></span>Figure 3.7: Propagation of pressure waves

The user can run the case and view results in dxFoam. The liquid flows out through the nozzle causing a wave to move along the nozzle. As it reaches the inlet to the tank, some of the wave is transmitted into the tank and some of it is reflected. While a wave is reflected up and down the inlet pipe, the waves transmitted into the tank expand and propagate through the tank. In Figure [3.7,](#page-71-0) the pressures are shown as contours so that the wave fronts are more clearly defined than if plotted as a normal isoline plot.

If the simulation is run for a long enough time for the reflected wave to return to the pipe, we can see that negative absolute pressure is detected. The modelling permits this and has some physical basis since liquids can support tension, *i.e.* negative pressures. In reality, however, impurities or dissolved gases in liquids act as sites for cavitation, or vapourisation/boiling, of the liquid due to the low pressure. Therefore in practical situations, we generally do not observe pressures falling below the vapourisation pressure of the liquid; not at least for longer than it takes for the cavitation process to occur.

## 3.3.5 Improving the solution by refining the mesh

Looking at the evolution of the resulting pressure field in time, we can clearly see the propagation of the pressure wave into the tank and numerous reflections from the inside walls. It is also obvious that the pressure wave is smeared over a number of cells. We shall now refine the mesh and reduce the time step to obtain a sharper front resolution. Simply edit the blockMeshDict and increase the number of cells by a factor of 4 in the x and  $y$


<span id="page-72-0"></span>Figure 3.8: Propagation of pressure waves with refined mesh

directions, *i.e.* block 0 becomes (120 80 1) from (30 20 1) and so on. Run blockMesh on this file. In addition, in order to maintain a Courant number below 1, the time step must be reduced accordingly to  $\Delta t = 10^{-7}$  s. The second simulation gives considerably better resolution of the pressure waves as shown in Figure [3.8.](#page-72-0)

# Chapter 4

# Multiphase flow

# 4.1 Breaking of a dam

Tutorial path:

• \$FOAM [TUTORIALS/multiphase/interFoam/laminar/damBreak/damBreak](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/multiphase/interFoam/laminar/damBreak/damBreak)

This example introduces the following OpenFOAM features for the first time:

- multiphase flow using VOF interface capturing method
- non-uniform initial conditions setup using setFields utility
- running case in parallel
- post-processing a case in parallel

#### 4.1.1 Problem specification

In this tutorial we shall solve a problem of simplified dam break in 2 dimensions using the interFoam.The feature of the problem is a transient flow of two fluids separated by a sharp interface, or free surface. The two-phase algorithm in interFoam is based on the volume of fluid (VOF) method in which a specie transport equation is used to determine the relative volume fraction of the two phases, or phase fraction  $\alpha$ , in each computational cell. Physical properties are calculated as weighted averages based on this fraction. The nature of the VOF method means that an interface between the species is not explicitly computed, but rather emerges as a property of the phase fraction field. Since the phase fraction can have any value between 0 and 1, the interface is never sharply defined, but occupies a volume around the region where a sharp interface should exist.

The test setup consists of a column of water at rest located behind a membrane on the left side of a tank. At time  $t = 0$  s, the membrane is removed and the column of water collapses. During the collapse, the water impacts an obstacle at the bottom of the tank and creates a complicated flow structure, including several captured pockets of air. The geometry and the initial setup is shown in Figure [4.1.](#page-76-0)

#### 4.1.2 Mesh generation

The user should go to the *damBreak* case in their **\$FOAM\_RUN/tutorials/multiphase/inter-**Foam/laminar directory. Generate the mesh running blockMesh as described previously. The damBreak mesh consist of 5 blocks; the *blockMeshDict* entries are given below.

```
17 scale 0.146;
18
19 vertices
20 (
21 (0 0 0)
22 (2\ 0\ 0)23 (2.16438 0 0)
24 (4 0 0)
25 (0 0.32876 0)
26 (2 0.32876 0)
27 (2.16438 0.32876 0)
28 (4 0.32876 0)
29 (0 4 0)
30 (2 4 0)
31 (2.16438 4 0)
32 (4 4 0)
33 (0 0 0.1)
34 (2 0 0.1)
35 \hspace{1.5cm} (2.16438 \ 0 \ 0.1)\frac{36}{36} \left(\frac{4}{6}\right)\left(\frac{0}{1}\right)<br>37 (0 0.3287)
         (0 \t0.32876 \t0.1)<br>(2 \t0.32876 \t0.1)\frac{3}{38} (2 0.32876 0.1)
39 (2.16438 0.32876 0.1)
```


<span id="page-76-0"></span>Figure 4.1: Geometry of the dam break.

```
40 (4 0.32876 0.1)
41 (0 4 0.1)
42 (2\;4\;0.1)43 (2.16438 4 0.1)
44 (4 4 0.1)
45 );
46
47 blocks
\frac{48}{49} (
49 hex (0 1 5 4 12 13 17 16) (23 8 1) simpleGrading (1 1 1)
50 hex (2 3 7 6 14 15 19 18) (19 8 1) simpleGrading (1 1 1)
51 hex (4 5 9 8 16 17 21 20) (23 42 1) simpleGrading (1 1 1)
         hex (5 6 10 9 17 18 22 21) (4 42 1) simpleGrading (1 1 1)
53 hex (6 7 11 10 18 19 23 22) (19 42 1) simpleGrading (1 1 1)
    );
55
56 edges
57 (
58 );
59
60 boundary
61 \t62leftWall<br>{
63 {
64 type wall;
\begin{array}{ccc}\n 65 & \text{faces} \\
 66 & \text{faces}\n \end{array}66 (
67 (0 12 16 4)
68 (4 16 20 8)
69 );
\begin{array}{c} 70 \\ 71 \end{array}71 rightWall
\frac{72}{73} {
73 type wall;<br>
74 faces
              f \overline{a} \overline{c} es
75 \over 7676 (7 19 15 3)
77 (11 23 19 7)
\begin{array}{ccc} 77 & & & \\ 78 & & & \\ 79 & & & \end{array} ) ;
79 }
\begin{array}{ccc}\n & \text{so} & \text{lowerWall} \\
 & \text{so} & \text{4}\n\end{array}81 {
82 type wall;
83 faces
84 (
85 (0 1 13 12)
86 \hspace{1.5cm} (1\;\;5\;\;17\;\;13)87 (5 6 18 17)
```

```
88 (2 14 18 6)
89 (2 3 15 14)
\begin{matrix}90\\91\end{matrix} );
91 }
92 atmosphere
93 {
94 type patch;<br>95 faces
\begin{array}{ccc}\n 95 \\
 96 \\
 \end{array} faces
96 (
97 (8 20 21 9)
98 (9 21 22 10)
\frac{99}{100} (10 22 23 11)
         \rightarrow\frac{101}{102}):
103
104 mergePatchPairs
\frac{105}{106}\mathcal{E}:
107
108 // ************************************************************************* //
```
#### 4.1.3 Boundary conditions

The user can examine the boundary geometry generated by blockMesh by viewing the boundary file in the *constant/polyMesh* directory. The file contains a list of 5 boundary patches: leftWall, rightWall, lowerWall, atmosphere and defaultFaces. The user should notice the type of the patches. The atmosphere is a standard patch, *i.e.* has no special attributes, merely an entity on which boundary conditions can be specified. The defaultFaces patch is empty since the patch normal is in the direction we will not solve in this 2D case. The leftWall, rightWall and lowerWall patches are each a wall. Like the plain patch, the wall type contains no geometric or topological information about the mesh and only differs from the plain patch in that it identifies the patch as a wall, should an application need to know, e.g. to apply special wall surface modelling.

A good example is that the interFoam solver includes modelling of surface tension at the contact point between the interface and wall surface. The models are applied by specifying the alphaContactAngle boundary condition on the alpha.water  $(\alpha)$  field. With it, the user must specify the following: a static contact angle, theta0  $\theta_0$ ; leading and trailing edge dynamic contact angles, thetaA  $\theta_A$  and thetaR  $\theta_R$  respectively; and a velocity scaling function for dynamic contact angle, uTheta.

In this tutorial we would like to ignore surface tension effects between the wall and interface. We can do this by setting the static contact angle,  $\theta_0 = 90^\circ$  and the velocity scaling function to 0. However, the simpler option which we shall choose here is to specify a zeroGradient type on alpha.water, rather than use the alphaContactAngle boundary condition.

The top boundary is free to the atmosphere so needs to permit both outflow and inflow according to the internal flow. We therefore use a combination of boundary conditions for pressure and velocity that does this while maintaining stability. They are:

- totalPressure which is a fixedValue condition calculated from specified total pressure p0 and local velocity U;
- pressureInletOutletVelocity, which applies zeroGradient on all components, except where there is inflow, in which case a fixedValue condition is applied to the *tangential* component;
- inletOutlet, which is a zeroGradient condition when flow outwards, fixedValue when flow is inwards.

At all wall boundaries, the fixedFluxPressure boundary condition is applied to the pressure field, which calculates the normal gradient from the local density gradient.

The defaultFaces patch representing the front and back planes of the 2D problem, is, as usual, an empty type.

# 4.1.4 Setting initial field

Unlike the previous cases, we shall now specify a non-uniform initial condition for the water phase fraction,  $\alpha$ , where

$$
\alpha = \begin{cases} 1 & \text{for the liquid phase} \\ 0 & \text{for the gas phase} \end{cases} \tag{4.1}
$$

This is achieved by running the setFields utility. It requires a setFieldsDict dictionary, located in the system directory, whose entries for this case are shown below.

```
17
18 defaultFieldValues
\frac{19}{20}volScalarFieldValue alpha.water 0
21 );
2223 regions
\frac{24}{25} (
25 boxToCell
26 {
\frac{1}{27} box (0 0 -1) (0.1461 0.292 1);
28 fieldValues<br>29 (
29 (
30 volScalarFieldValue alpha.water 1
31 );
32 }
33 );
34
35
36 // ************************************************************************* //
```
The defaultFieldValues sets the default value of the fields, *i.e.* the value the field takes unless specified otherwise in the regions sub-dictionary. That sub-dictionary contains a list of subdictionaries containing fieldValues that override the defaults in a specified region. The region is expressed in terms of a topoSetSource that creates a set of points, cells or faces based on some topological constraint. Here, boxToCell creates a bounding box within a vector minimum and maximum to define the set of cells of the liquid region. The phase fraction  $\alpha$  is defined as 1 in this region.

The setFields utility reads fields from file and, after re-calculating those fields, will write them back to file. Because the files are then overridden, it is recommended that a backup is made before setFields is executed. In the damBreak tutorial, the alpha.water field is initially stored as a backup *only*, named **alpha.water.orig.** Before running setFields, the user first needs to copy alpha.water.orig to alpha.water, e.g. by typing:

cp 0/alpha.water.orig 0/alpha.water

The user should then execute setFields as any other utility is executed. Using paraFoam, check that the initial alpha.water field corresponds to the desired distribution as in Figure [4.2.](#page-79-0)

# 4.1.5 Fluid properties

Let us examine the *transportProperties* file in the *constant* directory. Its dictionary contains the material properties for each fluid, separated into two subdictionaries *phase1* and *phase2*. The transport model for each phase is selected by the transportModel



Figure 4.2: Initial conditions for phase fraction alpha.water.

<span id="page-79-0"></span>keyword. The user should select Newtonian in which case the kinematic viscosity is single valued and specified under the keyword nu. The viscosity parameters for the other models, e.g.CrossPowerLaw, are specified within subdictionaries with the generic name <*model>Coeffs, i.e.CrossPowerLawCoeffs* in this example. The density is specified under the keyword rho.

The surface tension between the two phases is specified under the keyword sigma. The values used in this tutorial are listed in Table [4.1.](#page-79-1)

phase1 properties				
Kinematic viscosity	$\overline{m}^2$ s <sup>-1</sup>	ווח	$1.0 \times 10^{-6}$	
Density	$\text{kg m}^{-3}$	rho	$1.0 \times 10^{3}$	
phase2 properties				
Kinematic viscosity	$m^2 s^{-1}$	ווח	$1.48 \times 10^{-5}$	
Density	$\mathrm{kg}\,\mathrm{m}^{-3}$	rho	1.0	
Properties of both phases				
Surface tension	$N m^{-1}$	sigma	0.07	

<span id="page-79-1"></span>Table 4.1: Fluid properties for the damBreak tutorial

Gravitational acceleration is uniform across the domain and is specified in a file named g in the constant directory. Unlike a normal field file, e.g. U and  $p$ , g is a uniformDimensionedVectorField and so simply contains a set of dimensions and a value that represents  $(0, 9.81, 0)$  m s<sup>-2</sup> for this tutorial:

```
17
18 dimensions [0 1 -2 0 0 0 0];
19 value (0 -9.81 0);
20
21
22 // ************************************************************************* //
```
# 4.1.6 Turbulence modelling

As in the cavity example, the choice of turbulence modelling method is selectable at runtime through the simulationType keyword in *turbulenceProperties* dictionary. In this example, we wish to run without turbulence modelling so we set laminar:

```
17
18 simulationType laminar;
19
20
21 // ************************************************************************* //
```
#### 4.1.7 Time step control

Time step control is an important issue in free surface tracking since the surface-tracking algorithm is considerably more sensitive to the Courant number Co than in standard fluid flow calculations. Ideally, we should not exceed an upper limit  $Co \approx 0.5$  in the region of the interface. In some cases, where the propagation velocity is easy to predict, the user should specify a fixed time-step to satisfy the  $Co$  criterion. For more complex cases, this is considerably more difficult. interFoam therefore offers automatic adjustment of the time step as standard in the *controlDict*. The user should specify adjustTimeStep to be yes and the maximum Co for the phase fields, maxAlphaCo, and other fields, maxCo, to be 0.5. The upper limit on time step maxDeltaT can be set to a value that will not be exceeded in this simulation, e.g. 1.0.

By using automatic time step control, the steps themselves are never rounded to a convenient value. Consequently if we request that OpenFOAM saves results at a fixed number of time step intervals, the times at which results are saved are somewhat arbitrary. However even with automatic time step adjustment, OpenFOAM allows the user to specify that results are written at fixed times; in this case OpenFOAM forces the automatic time stepping procedure to adjust time steps so that it 'hits' on the exact times specified for write output. The user selects this with the adjustableRunTime option for writeControl in the *controlDict* dictionary. The *controlDict* dictionary entries should be:



#### 4.1.8 Discretisation schemes

The interFoam solver uses the multidimensional universal limiter for explicit solution (MULES) method, created by OpenCFD, to maintain boundedness of the phase fraction independent of underlying numerical scheme, mesh structure, etc. The choice of schemes for convection are therefore not restricted to those that are strongly stable or bounded, e.g. upwind differencing.

The convection schemes settings are made in the *divSchemes* sub-dictionary of the fvSchemes dictionary. In this example, the convection term in the momentum equation  $(\nabla \cdot (\rho \mathbf{U} \mathbf{U}))$ , denoted by the div(rhoPhi,U) keyword, uses Gauss linearUpwind grad(U) to produce good accuracy. The  $\nabla \cdot (\mathbf{U}\alpha)$  term, represented by the div(phi,alpha) keyword uses the vanLeer scheme. The  $\nabla \cdot (\mathbf{U}_{rb}\alpha)$  term, represented by the div(phirb, alpha) keyword, can similarly use the vanLeer scheme, but generally produces smoother interfaces using the linear scheme.

The other discretised terms use commonly employed schemes so that the *fvSchemes* dictionary entries should therefore be:

```
17
18 ddtSchemes
\frac{19}{20}20 default Euler;<br>21 }
    \mathcal{F}22
23 gradSchemes
\frac{24}{25} {
25 default Gauss linear;
    \mathcal{F}27
28 divSchemes
29 \{30 div(rhoPhi,U) Gauss linearUpwind grad(U);
31 div(phi,alpha) Gauss vanLeer;
32 div(phirb,alpha) Gauss linear;
33 div(((rho*nuEff)*dev2(T(grad(U))))) Gauss linear;
34 }
35
36 laplacianSchemes
37 {
38 default Gauss linear corrected;<br>39 }
    \mathcal{F}40
41 interpolationSchemes
\frac{42}{43} {
43 default linear;
    \lambda45
46 snGradSchemes
\frac{47}{48} {
48 default corrected;<br>49 }
    \mathcal{F}50
51
52 // ************************************************************************* //
```
#### 4.1.9 Linear-solver control

In the function, the PISO sub-dictionary contains elements that are specific to interFoam. There are the usual correctors to the momentum equation but also correctors to a PISO loop around the  $\alpha$  phase equation. Of particular interest are the nAlphaSubCycles and cAlpha keywords. nAlphaSubCycles represents the number of sub-cycles within the  $\alpha$ equation; sub-cycles are additional solutions to an equation within a given time step. It is used to enable the solution to be stable without reducing the time step and vastly increasing the solution time. Here we specify 2 sub-cycles, which means that the  $\alpha$ equation is solved in  $2\times$  half length time steps within each actual time step.

The cAlpha keyword is a factor that controls the compression of the interface where: 0 corresponds to no compression; 1 corresponds to conservative compression; and, anything larger than 1, relates to enhanced compression of the interface. We generally recommend a value of 1.0 which is employed in this example.

# 4.1.10 Running the code

Running of the code has been described in detail in previous tutorials. Try the following, that uses tee, a command that enables output to be written to both standard output and files:

cd \$FOAM RUN/tutorials/multiphase/interFoam/laminar/damBreak/damBreak interFoam | tee log

The code will now be run interactively, with a copy of output stored in the  $log$  file.

# 4.1.11 Post-processing

Post-processing of the results can now be done in the usual way. The user can monitor the development of the phase fraction  $\alpha$  alpha.water in time, e.g. see Figure [4.3.](#page-83-0)

# 4.1.12 Running in parallel

The results from the previous example are generated using a fairly coarse mesh. We now wish to increase the mesh resolution and re-run the case. The new case will typically take a few hours to run with a single processor so, should the user have access to multiple processors, we can demonstrate the parallel processing capability of OpenFOAM.

The user should first make a copy of the damBreak case, e.g. by

```
cd $FOAM RUN/tutorials/multiphase/interFoam/laminar/damBreak
mkdir damBreakFine
cp -r damBreak/0 damBreakFine
cp -r damBreak/system damBreakFine
cp -r damBreak/constant damBreakFine
```
Enter the new case directory and change the blocks description in the blockMeshDict dictionary to

```
blocks
(
    hex (0 1 5 4 12 13 17 16) (46 10 1) simpleGrading (1 1 1)
    hex (2 3 7 6 14 15 19 18) (40 10 1) simpleGrading (1 1 1)
    hex (4 5 9 8 16 17 21 20) (46 76 1) simpleGrading (1 2 1)
    hex (5 6 10 9 17 18 22 21) (4 76 1) simpleGrading (1 2 1)
    hex (6 7 11 10 18 19 23 22) (40 76 1) simpleGrading (1 2 1)
);
```
Here, the entry is presented as printed from the **blockMeshDict** file; in short the user must change the mesh densities, e.g. the 46 10 1 entry, and some of the mesh grading entries to 1 2 1. Once the dictionary is correct, generate the mesh.

As the mesh has now changed from the damBreak example, the user must re-initialise the phase field alpha. water in the  $\theta$  time directory since it contains a number of elements that is inconsistent with the new mesh. Note that there is no need to change the U and



<span id="page-83-0"></span>Figure 4.3: Snapshots of liquid phase  $\alpha$ .

p rgh fields since they are specified as uniform which is independent of the number of elements in the field. We wish to initialise the field with a sharp interface, *i.e.* it elements would have  $\alpha = 1$  or  $\alpha = 0$ . Updating the field with **mapFields** may produce interpolated values  $0 < \alpha < 1$  at the interface, so it is better to rerun the **setFields** utility. There is a backup copy of the initial uniform  $\alpha$  field named  $0/d$ s pha.water.org that the user should copy to  $0$ /alpha.water before running setFields:

#### cd \$FOAM RUN/tutorials/multiphase/interFoam/laminar/damBreak/damBreakFine cp -r 0/alpha.water.org 0/alpha.water setFields

The method of parallel computing used by OpenFOAM is known as domain decomposition, in which the geometry and associated fields are broken into pieces and allocated to separate processors for solution. The first step required to run a parallel case is therefore to decompose the domain using the decomposePar utility. There is a dictionary associated with decomposePar named decomposeParDict which is located in the system directory of the tutorial case; also, like with many utilities, a default dictionary can be found in the directory of the source code of the specific utility, *i.e.* in \$FOAM UTILITIES/parallelProcessing/decomposePar for this case.

The first entry is numberOfSubdomains which specifies the number of subdomains into which the case will be decomposed, usually corresponding to the number of processors available for the case.

In this tutorial, the method of decomposition should be simple and the corresponding simpleCoeffs should be edited according to the following criteria. The domain is split into pieces, or subdomains, in the  $x, y$  and  $z$  directions, the number of subdomains in each direction being given by the vector n. As this geometry is 2 dimensional, the 3rd direction, z, cannot be split, hence  $n_z$  must equal 1. The  $n_x$  and  $n_y$  components of **n** split the domain in the  $x$  and  $y$  directions and must be specified so that the number of subdomains specified by  $n_x$  and  $n_y$  equals the specified numberOfSubdomains, *i.e.*  $n_x n_y$  = numberOfSubdomains. It is beneficial to keep the number of cell faces adjoining the subdomains to a minimum so, for a square geometry, it is best to keep the split between the x and y directions should be fairly even. The **delta** keyword should be set to 0.001.

For example, let us assume we wish to run on 4 processors. We would set number-Of Subdomains to 4 and  $n = (2, 2, 1)$ . When running decompose Par, we can see from the screen messages that the decomposition is distributed fairly even between the processors.

The user should consult User Guide section [3.2](#page-63-0) for details of how to run a case in parallel; in this tutorial we merely present an example of running in parallel. We use the openMPI implementation of the standard message-passing interface (MPI). As a test here, the user can run in parallel on a single node, the local host only, by typing:

#### mpirun  $-$ np 4 interFoam  $-$ parallel > log &

The user may run on more nodes over a network by creating a file that lists the host names of the machines on which the case is to be run as described in User Guide section [3.2.2.](#page-64-0) The case should run in the background and the user can follow its progress by monitoring the *log* file as usual.

#### 4.1.13 Post-processing a case run in parallel

Once the case has completed running, the decomposed fields and mesh must be reassembled for post-processing using the reconstructPar utility. Simply execute it from the com-



Figure 4.4: Mesh of processor 2 in parallel processed case.

<span id="page-85-0"></span>mand line. The results from the fine mesh are shown in Figure [4.5.](#page-86-0) The user can see that the resolution of interface has improved significantly compared to the coarse mesh.

The user may also post-process a segment of the decomposed domain individually by simply treating the individual processor directory as a case in its own right. For example if the user starts paraFoam by

#### paraFoam -case processor1

then processor1 will appear as a case module in ParaView. Figure [4.4](#page-85-0) shows the mesh from processor 1 following the decomposition of the domain using the simple method.



<span id="page-86-0"></span>Figure 4.5: Snapshots of liquid phase  $\alpha$  with refined mesh.

Chapter 5

Stress analysis

# 5.1 Stress analysis of a plate with a hole

Tutorial path:

• \$FOAM\_[TUTORIALS/stressAnalysis/solidDisplacementFoam/plateHole](https://develop.openfoam.com/Development/OpenFOAM-plus/tree/master/tutorials/stressAnalysis/solidDisplacementFoam/plateHole)

This tutorial describes how to pre-process, run and post-process a case involving linearelastic, steady-state stress analysis on a square plate with a circular hole at its centre.

- thermal stress analysis using solidDisplacementFoam solver
- validation against the analytical solution

The plate dimensions are: side length 4 m and radius  $R = 0.5$  m. It is loaded with a uniform traction of  $\sigma = 10$  kPa over its left and right faces as shown in Figure [5.1.](#page-89-0) Two symmetry planes can be identified for this geometry and therefore the solution domain need only cover a quarter of the geometry, shown by the shaded area in Figure [5.1.](#page-89-0)



<span id="page-89-0"></span>Figure 5.1: Geometry of the plate with a hole.

# 5.1.1 Problem specification

The problem can be approximated as 2-dimensional since the load is applied in the plane of the plate. In a Cartesian coordinate system there are two possible assumptions to take in regard to the behaviour of the structure in the third dimension: (1) the plane stress condition, in which the stress components acting out of the 2D plane are assumed to be negligible; (2) the plane strain condition, in which the strain components out of the 2D plane are assumed negligible. The plane stress condition is appropriate for solids whose third dimension is thin as in this case; the plane strain condition is applicable for solids where the third dimension is thick.

An analytical solution exists for loading of an infinitely large, thin plate with a circular hole. The solution for the stress normal to the vertical plane of symmetry is

<span id="page-90-1"></span>
$$
\left(\sigma_{xx}\right)_{x=0} = \begin{cases} \sigma\left(1 + \frac{R^2}{2y^2} + \frac{3R^4}{2y^4}\right) & \text{for } |y| \ge R\\ 0 & \text{for } |y| < R \end{cases}
$$
\n
$$
(5.1)
$$

Results from the simulation will be compared with this solution. At the end of the tutorial, the user can: investigate the sensitivity of the solution to mesh resolution and mesh grading; and, increase the size of the plate in comparison to the hole to try to estimate the error in comparing the analytical solution for an infinite plate to the solution of this problem of a finite plate.

#### 5.1.2 Mesh generation

The domain consists of four blocks, some of which have arc-shaped edges. The block structure for the part of the mesh in the  $x - y$  plane is shown in Figure [5.2.](#page-90-0) As already mentioned in section [2.1.1.1,](#page-15-0) all geometries are generated in 3 dimensions in OpenFOAM even if the case is to be as a 2 dimensional problem. Therefore a dimension of the block in the  $z$  direction has to be chosen; here,  $0.5$  m is selected. It does not affect the solution since the traction boundary condition is specified as a stress rather than a force, thereby making the solution independent of the cross-sectional area.



<span id="page-90-0"></span>Figure 5.2: Block structure of the mesh for the plate with a hole.

The user should change into the plateHole case in the **\$FOAM\_RUN**/tutorials/stress-Analysis/solidDisplacementFoam directory and open the system/blockMeshDict file in an editor, as listed below

```
17 scale 1;
18
19 vertices<br>
20 (
\frac{20}{21}\begin{array}{ccc} 21 & (0.5 & 0) \\ 22 & (1 & 0) \end{array}22 (1 0 0)
23 (2 0 0)
24 (2 0.707107 0)
25 (0.707107 0.707107 0)
26 (0.353553 0.353553 0)
27 (2 \ 2 \ 0)28 (0.707107 2 0)
29 (0 2 0)
30 (0 1 0)
31 \hspace{1.5cm} (0 \hspace{.1cm} 0.5 \hspace{.1cm} 0)32 (0.5 0 0.5)
33 (1 0 0.5)
34 \quad (2 \ 0 \ 0.5)35 (2 0.707107 0.5)
36 (0.707107 0.707107 0.5)
37 (0.353553 0.353553 0.5)
38 (2 2 0.5)
39 (0.707107 2 0.5)
\begin{array}{cc} 40 & \text{(0 2 0.5)} \\ 41 & \text{(0 1 0.5)} \end{array}(0 \ 1 \ 0.5)\begin{pmatrix} 42 \\ 43 \end{pmatrix} (0 0.5 0.5)
     );
44
45 blocks
46 (
47 hex (5 4 9 10 16 15 20 21) (10 10 1) simpleGrading (1 1 1)
48 hex (0 1 4 5 11 12 15 16) (10 10 1) simpleGrading (1 1 1)
49 hex (1 2 3 4 12 13 14 15) (20 10 1) simpleGrading (1 1 1)
50 hex (4 3 6 7 15 14 17 18) (20 20 1) simpleGrading (1 1 1)
51 hex (9 4 7 8 20 15 18 19) (10 20 1) simpleGrading (1 1 1)
52 );
53
54 edges
\begin{array}{c} 55 \\ 56 \end{array} (
56 arc 0 5 (0.469846 0.17101 0)
57 arc 5 10 (0.17101 0.469846 0)
58 arc 1 4 (0.939693 0.34202 0)
59 arc 4 9 (0.34202 0.939693 0)
60 arc 11 16 (0.469846 0.17101 0.5)
61 arc 16 21 (0.17101 0.469846 0.5)
62 arc 12 15 (0.939693 0.34202 0.5)
\frac{63}{64} arc 15 20 (0.34202 0.939693 0.5)
     );
65
66 boundary
\begin{array}{cc} 67 & \text{C} \\ 68 & \text{C} \end{array}left
69 {
70 type symmetryPlane;<br>
71 faces
\begin{array}{ccc} 71 & & \text{faces} \\ 72 & & \text{(} \end{array}72 (
73 (8 9 20 19)
74 (9 10 21 20)
\begin{array}{cc} 75 & & \\ 76 & & \end{array} ) ;
76 }
          right
\frac{78}{79} {
79 type patch;<br>80 faces
\begin{array}{ccc}\n 80 & \text{faces} \\
 81 & \text{Gauss}\n \end{array}81 (
82 (2 3 14 13)
83 (3 6 17 14)
\begin{array}{ccc} 84 & & \\ 84 & & \\ 85 & & \end{array} );
          \mathcal{F}86 down
87 {
88 type symmetryPlane;<br>89 faces
\begin{array}{ccc}\n 89 & \text{faces} \\
 90 & \text{faces}\n \end{array}90 (
\frac{30}{91} (0 1 12 11)
\overline{12} \overline{2} 13 12)
\begin{matrix} 93 \\ 94 \end{matrix} );
94 }
          up<sup>1</sup>
\frac{96}{97} {
97 type patch;<br>98 faces
\begin{array}{ccc}\n 98 \\
 99\n \end{array} faces
99 (
100 (7 8 19 18)
101 (6 7 18 17)
```

```
102 );
103 }
104 hole
\frac{105}{106}type patch;
107 faces
108 (
109 (10 5 16 21)
110 (5 0 11 16)
111 );
\frac{112}{113}frontAndBack
114 {
115 type empty;<br>116 faces
116 faces
117 (
\frac{111}{118} (10 9 4 5)
119 (5 4 1 0)
120 (1 4 3 2)
121 (4 7 6 3)
122 \hspace{1.5cm} (4 \hspace{.1cm} 9 \hspace{.1cm} 8 \hspace{.1cm} 7)123 (21 16 15 20)
124 (16 11 12 15)
\begin{array}{cc}\n 125 \\
 126\n \end{array}
(12 13 14 15)<br>
\begin{array}{cc}\n 125 \\
 1417 \\
 18\n \end{array}126 (15 14 17 18)<br>127 (15 18 19 20)
\begin{array}{cc} 127 & (15 \ 18 \ 19 \ 20) \end{array}\rightarrow\frac{129}{130}) ;
131
132 mergePatchPairs
133 (
     \int ;
135
136 // ************************************************************************* //
```
Until now, we have only specified straight edges in the geometries of previous tutorials but here we need to specify curved edges. These are specified under the edges keyword entry which is a list of non-straight edges. The syntax of each list entry begins with the type of curve, including arc, simpleSpline, polyLine etc., described further in User Guide section 4.3.1. In this example, all the edges are circular and so can be specified by the arc keyword entry. The following entries are the labels of the start and end vertices of the arc and a point vector through which the circular arc passes.

The blocks in this **blockMeshDict** do not all have the same orientation. As can be seen in Figure [5.2](#page-90-0) the  $x_2$  direction of block 0 is equivalent to the  $-x_1$  direction for block 4. This means care must be taken when defining the number and distribution of cells in each block so that the cells match up at the block faces.

6 patches are defined: one for each side of the plate, one for the hole and one for the front and back planes. The left and down patches are both a symmetry plane. Since this is a geometric constraint, it is included in the definition of the mesh, rather than being purely a specification on the boundary condition of the fields. Therefore they are defined as such using a special symmetryPlane type as shown in the blockMeshDict.

The frontAndBack patch represents the plane which is ignored in a 2D case. Again this is a geometric constraint so is defined within the mesh, using the empty type as shown in the **blockMeshDict**. For further details of boundary types and geometric constraints, the user should refer to User Guide section 4.2.1.

The remaining patches are of the regular patch type. The mesh should be generated using blockMesh and can be viewed in paraFoam as described in section [2.1.2.](#page-20-0) It should appear as in Figure [5.3.](#page-93-0)

#### 5.1.2.1 Boundary and initial conditions

Once the mesh generation is complete, the initial field with boundary conditions must be set. For a stress analysis case without thermal stresses, only displacement D needs to be set. The  $0/D$  is as follows:



Figure 5.3: Mesh of the hole in a plate problem.

```
17 dimensions [0 1 0 0 0 0 0];
18
19 internalField uniform (0 0 0);
20
21 boundaryField
22 \sim 5
23 leftarrow{24} leftarrow{1}\frac{24}{25}type symmetryPlane;
\frac{26}{27}right
\frac{28}{29} {
               type tractionDisplacement:
30 traction uniform (10000 0 0);<br>31 pressure uniform 0;
                                   uniform 0;
\begin{array}{ccc} 32 & \text{value} \\ 33 & \text{} \end{array} value uniform (0\ 0\ 0);33 }
34 down
35 {
36 type symmetryPlane;<br>37 }
\frac{37}{38}\frac{1}{3}\begin{array}{c} 39 \\ 40 \end{array}type tractionDisplacement;
41 traction uniform (0 0 0);<br>
42 pressure uniform 0;
42 pressure uniform 0;
43 value uniform (0 0 0);
\frac{44}{45}hole
\frac{46}{47}type tractionDisplacement;
48 traction uniform (0 0 0);<br>
49 pressure uniform 0;
               pressure uniform 0;<br>value uniform (0)
50 value uniform (0 0 0);
\frac{51}{52}52 frontAndBack<br>53 f
\begin{array}{cc} 53 & \phantom{00} \overline{64} \end{array}type empty;
\begin{matrix} 55 & 3 \\ 56 & 3 \end{matrix}56 }
57
58 // ************************************************************************* //
```
Firstly, it can be seen that the displacement initial conditions are set to  $(0, 0, 0)$  m. The left and down patches must be both of symmetryPlane type since they are specified as such in the mesh description in the constant/polyMesh/boundary file. Similarly the frontAndBack patch is declared empty.

The other patches are traction boundary conditions, set by a specialist traction boundary type. The traction boundary conditions are specified by a linear combination of: (1) a boundary traction vector under keyword traction; (2) a pressure that produces a traction normal to the boundary surface that is defined as negative when pointing out of the surface, under keyword pressure. The up and hole patches are zero traction so the boundary traction and pressure are set to zero. For the right patch the traction should be (1e4, 0, 0) Pa and the pressure should be 0 Pa.

#### 5.1.2.2 Mechanical properties

The physical properties for the case are set in the mechanicalProperties dictionary in the constant directory. For this problem, we need to specify the mechanical properties of steel given in Table [5.1.](#page-94-0) In the mechanical properties dictionary, the user must also set planeStress to yes.



<span id="page-94-0"></span>Table 5.1: Mechanical properties for steel

#### 5.1.2.3 Thermal properties

The temperature field variable T is present in the solidDisplacementFoam solver since the user may opt to solve a thermal equation that is coupled with the momentum equation through the thermal stresses that are generated. The user specifies at run time whether OpenFOAM should solve the thermal equation by the thermalStress switch in the thermalProperties dictionary. This dictionary also sets the thermal properties for the case, e.g. for steel as listed in Table [5.2.](#page-94-1)

Property	Units	Keyword	Value
Specific heat capacity	$Jkg^{-1}K^{-1}$		434
Thermal conductivity	$Wm^{-1}K^{-1}$	k	60.5
Thermal expansion coeff.	$K^{-1}$	alpha	$1.1 \times 10^{-5}$

<span id="page-94-1"></span>Table 5.2: Thermal properties for steel

In this case we do not want to solve for the thermal equation. Therefore we must set the thermalStress keyword entry to no in the thermalProperties dictionary.

#### 5.1.2.4 Control

As before, the information relating to the control of the solution procedure are read in from the *controlDict* dictionary. For this case, the startTime is  $0$  s. The time step is not important since this is a steady state case; in this situation it is best to set the time step deltaT to 1 so it simply acts as an iteration counter for the steady-state case. The endTime, set to 100, then acts as a limit on the number of iterations. The writeInterval can be set to 20.

The *controlDict* entries are as follows:

17 18 application solidDisplacementFoam; 19 <sup>20</sup> startFrom startTime; 21



#### 5.1.2.5 Discretisation schemes and linear-solver control

Let us turn our attention to the  $f\nS$ chemes dictionary. Firstly, the problem we are analysing is steady-state so the user should select SteadyState for the time derivatives in timeScheme. This essentially switches off the time derivative terms. Not all solvers, especially in fluid dynamics, work for both steady-state and transient problems but solid-DisplacementFoam does work, since the base algorithm is the same for both types of simulation.

The momentum equation in linear-elastic stress analysis includes several explicit terms containing the gradient of displacement. The calculations benefit from accurate and smooth evaluation of the gradient. Normally, in the finite volume method the discretisation is based on Gauss's theorem The Gauss method is sufficiently accurate for most purposes but, in this case, the least squares method will be used. The user should therefore open the fvSchemes dictionary in the system directory and ensure the least Squares method is selected for the grad(U) gradient discretisation scheme in the gradSchemes sub-dictionary:

```
17
18 \t 19 \t 42d2d25chemes
19 {
20 default steadyState;
21 }
22
23 ddtSchemes
\frac{24}{25} {
25 default Euler;<br>26 }
     \mathcal{F}27
28 gradSchemes
\frac{29}{30} {
          default leastSquares;<br>
grad(D) leastSquares;
31 grad(D) leastSquares;
32 grad(T) leastSquares;<br>33 }
33 }
34
35 divSchemes
\frac{36}{37}37 default none;<br>38 div(sigmaD) Gauss
                             Gauss linear;
39 }
40
41 laplacianSchemes
42 \frac{1}{2}
```

```
43 default none;
44 laplacian(DD,D) Gauss linear corrected;
45 laplacian(DT,T) Gauss linear corrected;
46 }
47
48 interpolationSchemes
49 {
\begin{array}{ccc} 50 & \text{default} \\ 51 & \text{} \end{array}\mathcal{F}52
53 snGradSchemes
54 {
55 default none;
\frac{56}{56} }
57
58 // ************************************************************************* //
```
The functionary in the system directory controls the linear equation solvers and algorithms used in the solution. The user should first look at the solvers sub-dictionary and notice that the choice of solver for D is GAMG. The solver tolerance should be set to 10<sup>−</sup><sup>6</sup> for this problem. The solver relative tolerance, denoted by relTol, sets the required reduction in the residuals within each iteration. It is uneconomical to set a tight (low) relative tolerance within each iteration since a lot of terms in each equation are explicit and are updated as part of the segregated iterative procedure. Therefore a reasonable value for the relative tolerance is 0.01, or possibly even higher, say 0.1, or in some cases even 0.9 (as in this case).

```
17
18 solvers
\frac{19}{20}\begin{array}{cc} 20 & & \text{if } (D|T)^{11} \\ 21 & & \text{if } \end{array}21 {
<sup>22</sup> solver GAMG;<br><sup>23</sup> tolerance 1e-06;
23 tolerance 1e-0<br>24 relTol 0.9;
                  relTol<br>smoother
<sup>25</sup> smoother GaussSeidel;<br><sup>26</sup> mCellsInCoarsestLevel 20:
26 nCellsInCoarsestLevel 20;<br>27 }
      \rightarrow28 }
29
30 stressAnalysis
\frac{31}{32} {
32 compactNormalStress yes;<br>33 nCorrectors 1:
33 nCorrectors<br>34 D
                                    1e-06:
35 }
36
37
38 // ************************************************************************* //
```
The functionary contains a sub-dictionary, stress Analysis that contains some control parameters specific to the application solver. Firstly there is nCorrectors which specifies the number of outer loops around the complete system of equations, including traction boundary conditions within each time step. Since this problem is steady-state, we are performing a set of iterations towards a converged solution with the 'time step' acting as an iteration counter. We can therefore set nCorrectors to 1.

The D keyword specifies a convergence tolerance for the outer iteration loop, *i.e.* sets a level of initial residual below which solving will cease. It should be set to the desired solver tolerance specified earlier,  $10^{-6}$  for this problem.

#### 5.1.3 Running the code

The user should run the code here in the background from the command line as specified below, so he/she can look at convergence information in the log file afterwards.

```
cd $FOAM RUN/tutorials/stressAnalysis/solidDisplacementFoam/plateHole
solidDisplacementFoam > log &
```
The user should check the convergence information by viewing the generated  $\log$  file which shows the number of iterations and the initial and final residuals of the displacement in each direction being solved. The final residual should always be less than 0.9 times the initial residual as this iteration tolerance set. Once both initial residuals have dropped below the convergence tolerance of  $10^{-6}$  the run has converged and can be stopped by killing the batch job.

# <span id="page-97-1"></span>5.1.4 Post-processing

Post processing can be performed as in section [2.1.4.](#page-22-0) The solidDisplacementFoam solver outputs the stress field  $\sigma$  as a symmetric tensor field sigma. This is consistent with the way variables are usually represented in OpenFOAM solvers by the mathematical symbol by which they are represented; in the case of Greek symbols, the variable is named phonetically.

For post-processing individual scalar field components,  $\sigma_{xx}$ ,  $\sigma_{xy}$  etc., can be generated by running the postProcess utility as before in section [2.1.5.7,](#page-29-0) this time on sigma:

```
postProcess -func 'components(sigma)'
```
Components named sigmaxx, sigmaxy etc. are written to time directories of the case. The  $\sigma_{xx}$  stresses can be viewed in **paraFoam** as shown in Figure [5.4.](#page-97-0)



<span id="page-97-0"></span>Figure 5.4:  $\sigma_{xx}$  stress field in the plate with hole.

We would like to compare the analytical solution of Equation [5.1](#page-90-1) to our solution. We therefore must output a set of data of  $\sigma_{xx}$  along the left edge symmetry plane of our domain. The user may generate the required graph data using the postProcess utility, using a sets function object. The utility can be driven from a user-supplied file located in the system directory, whose entries are summarised in User Guide Table 7.3. The sample line specified in sets is set between  $(0.0, 0.5, 0.25)$  and  $(0.0, 2.0, 0.25)$ , and the fields are specified in the fields list:

```
8
9 singleGraph
\frac{10}{11} {
11 start (0 0.5 0.25);
12 end (0 2 0.25);
13 fields (sigmaxx);
14
15 #includeEtc "caseDicts/postProcessing/graphs/sampleDict.cfg"
```


<span id="page-98-0"></span>Figure 5.5: Normal stress along the vertical symmetry  $(\sigma_{xx})_{x=0}$ 

```
17 setConfig
18 \t 19axis y;
20 }
21
22 // Must be last entry
23 #includeEtc "caseDicts/postProcessing/graphs/graph.cfg"
24 }
25
26 // ************************************************************************* //
```
The writeFormat is raw 2 column format. The data is written into files within time subdirectories of a sets directory, e.g. the data at  $t = 100$  s is found within the file sets/100/leftPatch sigmaxx.xy. In an application such as GnuPlot, one could type the following at the command prompt would be sufficient to plot both the numerical data and analytical solution:

plot [0.5:2] [0:] 'sets/100/leftPatch sigmaxx.xy', 1e4\*(1+(0.125/(x\*\*2))+(0.09375/(x\*\*4)))

An example plot is shown in Figure [5.5.](#page-98-0)

# 5.1.5 Exercises

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The user may wish to experiment with solidDisplacementFoam by trying the following exercises:

#### 5.1.5.1 Increasing mesh resolution

Increase the mesh resolution in each of the x and y directions. Use mapFields to map the final coarse mesh results from section [5.1.4](#page-97-1) to the initial conditions for the fine mesh.

#### 5.1.5.2 Introducing mesh grading

Grade the mesh so that the cells near the hole are finer than those away from the hole. Design the mesh so that the ratio of sizes between adjacent cells is no more than 1.1 and so that the ratio of cell sizes between blocks is similar to the ratios within blocks. Mesh grading is described in section [2.1.6.](#page-32-0) Again use mapFields to map the final coarse mesh results from section [5.1.4](#page-97-1) to the initial conditions for the graded mesh. Compare the results with those from the analytical solution and previous calculations. Can this solution be improved upon using the same number of cells with a different solution?

#### 5.1.5.3 Changing the plate size

The analytical solution is for an infinitely large plate with a finite sized hole in it. Therefore this solution is not completely accurate for a finite sized plate. To estimate the error, increase the plate size while maintaining the hole size at the same value.

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